

UNIVERSITEIT VAN AMSTERDAM INSTITUTE FOR LOGIC, LANGUAGE AND COMPUTATION

# Reasoning and Formal Modelling for Forensic Science 2010/2011; 2nd Semester Prof. Dr. Benedikt Löwe

# Werkcollege Exercises #2

Please start thinking about these exercises before the next *werkcollege* on Tuesday, 15 February, 11am, room A1.04. The exercises will be discussed in class with active student participation: you will get some extra time to think about them, and then present the solutions in front of the class.

# Exercise 5.

Check whether the following formulas are valid:

• 
$$\neg(\neg p \lor \neg q) \to q$$
,

•  $((p \land q) \rightarrow r) \rightarrow (((q \rightarrow p) \land q) \rightarrow r),$ •  $(p \land q) \leftrightarrow \neg (p \lor q),$ •  $\neg \neg (p \land q) \leftrightarrow \neg (\neg p \land \neg q).$ 

• 
$$(p \land q) \leftrightarrow \neg (p \lor q),$$

# Exercise 6.

Consider the binary connective given by the truth table

$$\begin{array}{c|c} T & F \\ \hline T & F & T \\ F & T & T. \end{array}$$

It is sometimes called "NAND". Can you explain why? There is a formally provable result behind this explanation. State it and prove it.

# Exercise 7.

In the lecture, we have always worked with only two truth values: true and false. Suppose for a moment that we allow three truth values: true, undecided and false. How many truth-functional binary connectives with three truth values exist? (Compare Exercise 1.) Come up with reasonable truth tables for conjunction ("and") and disjunction ("or") in this setting.