# OP-SFNET - Volume 16, Number 2 - March 15, 2009

#### Editors:

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The Electronic News Net of the SIAM Activity Group on Orthogonal Polynomials and Special Functions <a href="http://math.nist.gov/opsf/">http://math.nist.gov/opsf/</a>

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#### Today's Topics:

- 1. Ancient Chinese Mathematics
- 2. Preprints in arXiv.org
- 3. About the Activity Group
- 4. Submitting contributions to OP-SF NET

#### Calendar of Events:

#### March 21-24, 2009

Workshop "Approximation Theory and Signal Analysis" dedicated to Professor Paul Leo Butzer on the occasion of his 80th birthday Lindau (Lake Constance), Germany 15.6, #2 16.1, #1 http://ibb.helmholtz-muenchen.de/~biomath/workshop\_atsa.html

#### March 25-30, 2009

Random Matrices and Integrability: From Theory to Application, Yad Hashmona, Israel <a href="http://www.hit.ac.il/staff/kanzieper/yad8">http://www.hit.ac.il/staff/kanzieper/yad8</a>

#### April 13-25, 2009

CIMPA-Unesco-Tunisia School "Analytical and Probabilistic Aspects of Dunkl Theory", Monastir, Tunisia 15.5 #6 http://www.cimpa-icpam.org/Anglais/2009Prog/Tunisia09.html

### April 19--26, 2009 - \*\*\*\*CANCELLED\*\*\*\*

NoDIA-2009: Nonlinear Differential Equations, Integrability and Applications - Cape Town, South Africa.

### June 8-12, 2009

Sixth International Conference on Computational Methods and Function Theory, Ankara, Turkey.

15.4 #2

http://www.bilkent.edu.tr/~cmft/

### June 14-20, 2009

47th International Symposium on Functional Equations Gargnano, Italy. GianLuigi.Forti@mat.unimi.it

### June 15-18, 2009

3rd International Conference on Mathematics & Statistics, Athens, Greece <a href="http://www.atiner.gr/docs/Mathematics.htm">http://www.atiner.gr/docs/Mathematics.htm</a>

### June 25-28, 2009

International Conference on Applied Analysis and Scientific Computation Shanghai Normal University, Shanghai, China 15.5 #4 http://mathsc.shnu.edu.cn/conference/index.htm

### June 29 - July 3, 2009

Workshop "Discrete systems and special functions", Newton Institute for Mathematical Sciences, Cambridge, UK. 15.5 #9 http://www.newton.ac.uk/programmes/DIS/ws.htm

#### July 6-10, 2009

2009 SIAM Annual Meeting, Denver, Colorado, USA <a href="http://www.siam.org/meetings/an09/">http://www.siam.org/meetings/an09/</a>

### July 20-24, 2009

FPSAC'09 -21st Annual International Conference on Formal Power Series and Algebraic Combinatorics, Hagenberg, Austria 15.5 #3

http://www.risc.jku.at/conferences/fpsac2009

#### July 20-25, 2009

10th Symposium on Orthogonal Polynomials, Special Functions and Applications (OPSFA-10), Leuven, Belgium

15.5 #2

16.1 #2

http://wis.kuleuven.be/OPSFA/OPSFA10.html

#### September 4-9, 2009

2nd Dolomites Workshop on Constructive Approximation and Applications" (DWCAA09), Alba di Canazei (Trento), Italy http://www.math.unipd.it/~dwcaa09

#### September 13-19, 2009

International Conference on Functional Equations and Inequalities, Krakow, Poland

http://mat.ap.krakow.pl/icfei/13ICFEI/index.php

#### September 24-30, 2009

6th Maratea Conference on Functional Analysis and Approximation Theory (FAAT2009), Acquafreda di Maratea, Italy http://www.dm.uniba.it/faat2009

## Topic #1 ----- OP-SF NET 16.2 ----- March 15, 2009

From: OP-SF NET Editors

Subject: Ancient Chinese Mathematics

In the January/February 2009 issue of SIAM News Philip Davis wrote a review of Simon Winchester's "The Man Who Loved China". This book describes the life of Joseph Needham, a distinguished biochemist from Cambridge University, England, and author of the multi-volume "Science and Civilization in China" (Cambridge University Press). Volume 3 (1959) contains 168 pages on ancient Chinese mathematics, which is why Needham is a person of particular interest to Davis and to us. The reviewer discusses not just the book under review, but has interesting things to say about the critical reception of Needham's work by later historians of science. For criticisms of Needham specific to mathematics, Davis turns to the book "A History of Chinese Mathematics" by Jean-Claude Martzloff, which, in his outsider's judgment, is currently the best general history of the subject; it places the mathematics strongly within the ancient Chinese cultural context.

Tom Koornwinder wrote the following reaction to Davis' book review as a Letter to the Editor. This reaction will appear in the next issue of SIAM News.

With interest I read Philip Davis's book review "Why Didn't They ...?" in SIAM News (January/February 2009, page 6). Encouraged by his recommendation, I borrowed the book A History of Chinese Mathematics by J.-C. Martzloff from the library. However, I am somewhat disappointed by the coverage of Zhu Shijie (ca. 1300) in this book.

See Needham, Vol. 3, pp. 138, 139 for formulas due to Zhu Shijie (written by Needham as Chu Shih-Chieh), which were reformulated by Askey (Orthogonal Polynomials and Special Functions, SIAM, 1975, pp. 59, 60) as Vandermonde's sum (the explicit summation of the terminating Gauss hypergeometric function of argument 1). Therefore, Vandermonde's sum is now called the Chu-Vandermonde sum by the special functions community.

Martzloff, however, does not mention this work by Zhu Shijie. He does treat in some detail in Chapter 18 the much later (19th century) work of Li Shanlan. The formula (18.1) there can be reformulated as a special case of Saalschutz's formula for hypergeometric  ${}_3F_2(1)$ . According to secondary sources quoted by Askey, this formula (18.1), too, seems to go back to Zhu Shijie. However, the only mention of Zhu Shijie in Chapter 18 is in a quote from the preface of the book by Li Shanlan:

"Master Zhu Shijie from the Yuan dynasty is the only one who has made use of the prescriptions relating the piling up of heaps in the chapters of his Siyuan yujian entitled ..... But his intention was only to expound the algebra and for that reason he presents the piling up of heaps neither precisely nor methodically."

Martzloff speculates in this chapter about influences on Li Shanlan by Western mathematical work. But if some of Li Shanlan's formulas go back to Zhu Shijie, then Western influence on this part is less probable.

Needham, after the formulas quoted by Askey, hints at "many other formulas of similar nature" given by Chu Shih-Chieh. I would like to see a transcription of this part of Chu's writings, to learn what further treasures his work might contain.

Tom Koornwinder, Korteweg-de Vries Institute for Mathematics, University of Amsterdam.

## Topic #2 ----- OP-SF NET 16.2 ----- March 15, 2009

From: OP-SF NET Editors Subject: Preprints in arXiv.org

The following preprints related to the fields of orthogonal polynomials and special functions were posted or cross-listed to one of the subcategories of arXiv.org mostly during January and February 2009.

http://arxiv.org/abs/0901.0054

Counting decomposable univariate polynomials

Authors: Joachim von zur Gathen

http://arxiv.org/abs/0901.0190 Airy functions over local fields

Authors: Rahul N. Fernandez, V. S. Varadarajan, David Weisbart

http://arxiv.org/abs/0901.0249

On the q-Extensions of the Bernoulli and Euler Numbers, Related Identities and Lerch Zeta Function

Authors: Taekyun Kim, Younghee Kim, kyoungwon Hwang

http://arxiv.org/abs/0901.0324

Beta Jacobi processes Authors: Nizar Demni

http://arxiv.org/abs/0901.0353

New approach to q-Genocch, Euler numbers and polynomials and their

interpolation functions Authors: Taekyun Kim

Convergence of ray sequences of Pade approximants to 2F1(a,1;c;z), c>a>0

Authors: K Driver, K Jordaan

### http://arxiv.org/abs/0901.0746

O(N) colour-flavour transformations and characteristic polynomials of real random matrices

Authors: Yi Wei, Boris A. Khoruzhenko

### http://arxiv.org/abs/0901.0837

Structural Relations of Harmonic Sums and Mellin Transforms at Weight w=6

Authors: Johannes Blümlein

#### http://arxiv.org/abs/0901.0897

Gap Probabilities in Non-Hermitian Random Matrix Theory

Authors: G. Akemann, M.J. Phillips, L. Shifrin

### http://arxiv.org/abs/0901.0947

Orthogonal polynomials on the unit circle, \$q\$-Gamma weights, and discrete

Painlevé equations

Authors: Philippe Biane

#### http://arxiv.org/abs/0901.0982

Complex Hadamard matrices from Sylvester inverse orthogonal matrices

Authors: Petre Dita

### http://arxiv.org/abs/0901.1104

Mathieu's series: inequalities, asymptotics and positive definiteness

Authors: Viktor P. Zastavnyi

#### http://arxiv.org/abs/0901.1379

Pseudo-factorials, elliptic functions, and continued fractions

Authors: Roland Bacher, Philippe Flajolet

#### http://arxiv.org/abs/0901.1548

On Gram's law in the theory of the Riemann zeta function

Authors: Jan Mozer

#### http://arxiv.org/abs/0901.1697

Note on the generalization of the higher order q-Genocchi numbers and q-Euler

Authors: Taekyun Kim, Young-hee Kim, Kyoung-won Hwang

### http://arxiv.org/abs/0901.1725

Inequalities for the eigenvalues of non-selfadjoint Jacobi operators

Authors: Marcel Hansmann, Guy Katriel

Hankel determinants of Dirichlet series

Authors: H. Monien

http://arxiv.org/abs/0901.2006

The fermionic p-adic integrals on Zp associated with extended q-Euler numbers

and polynomials Authors: Taekyun Kim

http://arxiv.org/abs/0901.2083

Some applications of the Stieltjes constants

Authors: Donal F. Connon

http://arxiv.org/abs/0901.2424

A new type of critical behaviour in random matrix models

Authors: R. Flume, A. Klitz

http://arxiv.org/abs/0901.2473

Higher order analogues of the Tracy-Widom distribution and the Painleve II

hierarchy

Authors: T. Claeys, A. Its, I. Krasovsky

http://arxiv.org/abs/0901.2655

On Non-central Stirling Numbers of the First Kind

Authors: Milan Janjic

http://arxiv.org/abs/0901.2940

Orthogonality of Jacobi and Laguerre polynomials for general parameters via the

Hadamard finite part Authors: Rodica D. Costin

http://arxiv.org/abs/0901.3328

On the Geometric Interpretation of the Complex Fourier Transforms of a Class

of Exponential Functions

**Authors: Jeremy Williams** 

http://arxiv.org/abs/0901.3377

Mean Staircase of the Riemann Zeros: a comment on the Lambert W function

and an algebraic aspect

Authors: Davide a Marca, Stefano Beltraminelli, Danilo Merlini

http://arxiv.org/abs/0901.3379

Zonal polynomials and hypergeometric functions of quaternion matrix argument

Authors: Fei Li, Yifeng Xue

http://arxiv.org/abs/0901.3452

Ramanujan Summation and the Exponential Generating Function \$

 $\sum_{k=0}^{\int x_{k}}{k!}\zeta ^{\phi(-k)}$ 

Authors: B. Candelpergher, H. Gopalkrishna Gadiyar, R. Padma

On the Zeros of the Complex Fourier Transforms of a Class of Exponential

**Functions** 

**Authors: Jeremy Williams** 

### http://arxiv.org/abs/0901.3970

Integrals of products of Hermite functions

Authors: Wei-Min Wang

#### http://arxiv.org/abs/0901.3973

Jacob's ladders and the almost exact asymptotic representation of the Hardy-

Littlewood integral Authors: Jan Moser

#### http://arxiv.org/abs/0901.4176

The sl\_3 Selberg integral Authors: S. Ole Warnaar

#### http://arxiv.org/abs/0901.4501

Some properties of deformed \$q\$-numbers

Authors: Thierry C. Petit Lobão, Pedro G. S. Cardoso, Suani T. R. Pinho, Ernesto

P. Borges

#### http://arxiv.org/abs/0901.4564

The p-adic valuations of sequences counting alternating sign matrices

Authors: Xinyu Sun, Victor H. Moll

### http://arxiv.org/abs/0901.4680

Hankel determinants of Schroeder-like numbers

Authors: Johann Cigler

#### http://arxiv.org/abs/0901.4698

Hankel determinants of q-exponential polynomials

Authors: Johann Cigler

#### http://arxiv.org/abs/0901.2244

Matrix valued Szego polynomials and quantum random walks Authors: M. J. Cantero, F. A. Grünbaum, L. Moral, L. Velazquez

#### http://arxiv.org/abs/0901.2717

On the Spatial Asymptotics of Solutions of the Toda Lattice

Authors: Gerald Teschl

#### http://arxiv.org/abs/0901.4716

Feynman Diagrams, Differential Reduction, and Hypergeometric Functions Authors: M. Yu. Kalmykov (Hamburg U., Inst. Theor. Phys. II & Dubna, JINR), V. V. Bytev (Hamburg U., Inst. Theor. Phys. II & Dubna, JINR) Bernd A. Kniehl (Hamburg U., Inst. Theor. Phys. II), B.F.L. Ward (Baylor U.), S.A. Yost (Citadel Military Coll.)

Polynomial solutions of differential-difference equations Authors: Diego Dominici, Kathy Driver, Kerstin Jordaan

http://arxiv.org/abs/0902.0051

Compatibility of the Theta correspondence with the Whittaker functors Authors: Vincent Lafforgue (University Paris 6), Sergey Lysenko (University Nancy

1)

http://arxiv.org/abs/0902.0054

On generalized Cauchy-Stieltjes transforms of some Beta distributions

Authors: Nizar Demni

http://arxiv.org/abs/0902.0116

A passage to the Poisson-Dirichlet through the Bessel square processes

Authors: Soumik Pal

http://arxiv.org/abs/0902.0193

Critical measures, quadratic differentials, and weak limits of zeros of Stieltjes

polynomials

Authors: A. Martinez-Finkelshtein, E. A. Rakhmanov

http://arxiv.org/abs/0902.0380

Special Functions Related to Dedekind Type DC-Sums and their Applications

Authors: Yilmaz Simsek

http://arxiv.org/abs/0902.0413

On the number of real critical points of logarithmic derivatives and the Hawaii

conjecture

Authors: Mikhail Tyaglov

http://arxiv.org/abs/0902.0451

Cariñena polynomials are Jacobi polynomials

Authors: C. Vignat, P.W. Lamberti

http://arxiv.org/abs/0902.0621

Basic hypergeometric functions as limits of elliptic hypergeometric functions

Authors: Fokko van de Bult, Eric Rains

http://arxiv.org/abs/0902.0789

The series limit of sum\_k  $1/[k \log k (\log \log k)^2]$ 

Authors: Richard J. Mathar

http://arxiv.org/abs/0902.0797

De Toda à KdV

Authors: Dario Bambusi, Thomas Kappeler, Thierry Paul (DMA)

http://arxiv.org/abs/0902.0804

On a nonlinear recurrent relation

Authors: Dong Li

Computing the smallest eigenvalue of large ill-conditioned Hankel matrices

Authors: Niall Emmart, Charles C. Weems, Yang Chen

### http://arxiv.org/abs/0902.0910

A novel analytical operator method to solve linear ordinary differential equations with variable coefficients

Authors: Wrick Sengupta

### http://arxiv.org/abs/0902.1027

Condensation of the roots of real random polynomials on the real axis

Authors: Gregory Schehr, Satya N. Majumdar

## http://arxiv.org/abs/0902.1058

Multiple orthogonal polynomial ensembles

Authors: Arno B.J. Kuijlaars

### http://arxiv.org/abs/0902.1650

A simple approach to some Hankel determinants

Authors: Johann Cigler

#### http://arxiv.org/abs/0902.1691

A recurrence relation for the Li/Keiper constants in terms of the Stieltjes

constants

Authors: Donal F. Connon

### http://arxiv.org/abs/0902.2099

Recurrence formulas for Macdonald polynomials of type A

Authors: Michel Lassalle, Michael J. Schlosser

#### http://arxiv.org/abs/0902.2188

Some integrals involving the Stieltjes constants

Authors: Donal F. Connon

#### http://arxiv.org/abs/0902.2390

Group Classification of a family of second-order differential equations

Authors: J.C. Ndogmo

#### http://arxiv.org/abs/0902.2513

A complete solution to an open problem relating to an inequality for ratios of gamma functions

Authors: Feng Qi, Bai-Ni Guo

### http://arxiv.org/abs/0902.2514

Bounds for the ratio of two gamma functions--From Wendel's limit to Elezović-

Giordano-Pečarić's theorem

Authors: Feng Qi

A short proof of monotonicity of a function involving the psi and exponential functions

Authors: Feng Qi, Bai-Ni Guo

http://arxiv.org/abs/0902.2588

Concise sharpening and generalizations of Shafer's inequality for the arc sine

function

Authors: Feng Qi, Bai-Ni Guo

http://arxiv.org/abs/0902.2991

Generalized Heun and Lamé's equations: factorization Authors: Mahouton Norbert Hounkonnou, André Ronveaux

http://arxiv.org/abs/0902.3073

Log-convexity and log-concavity of hypergeometric-like functions

Authors: D.Karp, S.M. Sitnik

http://arxiv.org/abs/0902.3190 On a polynomial zeta function Authors: Sergio L. Cacciatori

http://arxiv.org/abs/0902.3440

Curves defined by Chebyshev polynomials

Authors: Gene Freudenburg, Jenna Freudenburg

http://arxiv.org/abs/0902.3870

Asymptotic Independence of the Extreme Eigenvalues of GUE

Authors: Folkmar Bornemann

http://arxiv.org/abs/0902.3953

Nearest lambda g-multiple fractions

Authors: Dieter Mayer, Tobias Mühlenbruch

http://arxiv.org/abs/0902.4064

Differential equations for deformed Laguerre polynomials

Authors: Peter J. Forrester, Christopher M. Ormerod

http://arxiv.org/abs/0902.4169

Arithmetic theory of q-difference equations ( $G_q$ -functions and q-difference

modules of type G, global q-Gevrey series)

Authors: Lucia Di Vizio

http://arxiv.org/abs/0902.4608

Quantum alpha-determinants and q-deformed hypergeometric polynomials

Authors: Kazufumi Kimoto

http://arxiv.org/abs/0902.4732

On the number zeta(3) Authors: L.A.Gutnik

Coherent states of a particle in magnetic field and Stieltjes moment problem Authors: J.P. Gazeau, M.C. Baldiotti, D.M. Gitman

# Topic #3 ----- OP-SF NET 16.2 ----- March 15, 2009

From: OP-SF NET Editors

Subject: About the Activity Group

The SIAM Activity Group on Orthogonal Polynomials and Special Functions consists of a broad set of mathematicians, both pure and applied. The Group also includes engineers and scientists, students as well as experts. We have around 140 members scattered about in more than 20 countries. Whatever your specialty might be, we welcome your participation in this classical, and yet modern, topic. Our WWW home page is:

http://math.nist.gov/opsf/

This is a convenient point of entry to all the services provided by the Group. Our Webmaster is Bonita Saunders (bonita.saunders@nist.gov).

The Activity Group sponsors OP-SF NET, which is transmitted periodically by SIAM. It is provided as a free public service; membership in SIAM is not required. The OP-SF Net Editors are Diego Dominici (dominicd@newpaltz.edu) and Martin Muldoon (muldoon@yorku.ca).

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For several years the Activity Group sponsored a printed Newsletter, most recently edited by Rafael Yanez. Back issues are accessible at: http://www.mathematik.uni-kassel.de/~koepf/siam.html

SIAM has several categories of membership, including low-cost categories for students and residents of developing countries. For current information on SIAM and Activity Group membership, contact:

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http://www.siam.org/membership/outreachmem.htm

Finally, the Activity Group operates an email discussion group, called OP-SF Talk. To subscribe, send the email message

subscribe opsftalk Your Name

to listproc@nist.gov. To contribute an item to the discussion, send email to opsftalk@nist.gov. The archive of all messages is accessible at:

http://math.nist.gov/opsftalk/archive

## Topic #4 ----- OP-SF NET 16.2 ----- March 15, 2009

From: OP-SF NET Editors

Subject: Submitting contributions to OP-SF NET

To contribute a news item to OP-SF NET, send email to poly@siam.org with a copy to one of the OP-SF Editors <a href="mailto:dominicd@newpaltz.edu">dominicd@newpaltz.edu</a> or <a href="mailto:muldoon@yorku.ca">muldoon@yorku.ca</a>. Contributions to OP-SF NET 16.3 should be sent by May 1, 2009.

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http://www.math.ohio-state.edu/JAT/DATA/OPSFNET/opsfnet.html

http://math.nist.gov/opsfnet/archive

WWW home page of this Activity Group:

http://math.nist.gov/opsf/

Information on joining SIAM and this activity group: service@siam.org

The elected Officers of the Activity Group (2008-2010) are:

Francisco J. Marcellán , Chair Peter A. Clarkson, Vice Chair Daniel W. Lozier, Secretary

Peter A. McCoy, Program Director

The appointed officers are:

Diego Dominici, OP-SF NET co-editor Martin Muldoon, OP-SF NET co-editor

Bonita Saunders, Webmaster