# O P - S F N E T - Volume 16, Number 2 - March 15, 2009 

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The Electronic News Net of the
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Today's Topics:

1. Ancient Chinese Mathematics
2. Preprints in arXiv.org
3. About the Activity Group
4. Submitting contributions to OP-SF NET

## Calendar of Events:

March 21-24, 2009
Workshop "Approximation Theory and Signal Analysis"
dedicated to Professor Paul Leo Butzer on the occasion of his 80th birthday
Lindau (Lake Constance), Germany 15.6, \#2 16.1, \#1
http://ibb.helmholtz-muenchen.de/~biomath/workshop_atsa.html
March 25-30, 2009
Random Matrices and Integrability: From Theory to Application, Yad Hashmona, Israel
http://www.hit.ac.il/staff/kanzieper/yad8
April 13-25, 2009
CIMPA-Unesco-Tunisia School "Analytical and Probabilistic Aspects of Dunkl Theory", Monastir, Tunisia 15.5 \#6
http://www.cimpa-icpam.org/Anglais/2009Prog/Tunisia09.html
April 19-26, 2009 - ****CANCELLED****
NoDIA-2009: Nonlinear Differential Equations, Integrability and Applications Cape Town, South Africa.

June 8-12, 2009
Sixth International Conference on Computational Methods and Function Theory, Ankara, Turkey. 15.4 \#2
http://www.bilkent.edu.tr/~cmft/
June 14-20, 2009
47th International Symposium on Functional Equations Gargnano, Italy. GianLuigi.Forti@mat.unimi.it

## June 15-18, 2009

3rd International Conference on Mathematics \& Statistics, Athens, Greece http://www.atiner.gr/docs/Mathematics.htm

June 25-28, 2009
International Conference on Applied Analysis and Scientific Computation Shanghai Normal University, Shanghai, China 15.5 \#4
http://mathsc.shnu.edu.cn/conference/index.htm
June 29 - July 3, 2009
Workshop "Discrete systems and special functions", Newton Institute for Mathematical Sciences, Cambridge, UK.
15.5 \#9 http://www.newton.ac.uk/programmes/DIS/ws.htm

July 6-10, 2009
2009 SIAM Annual Meeting, Denver, Colorado, USA
http://www.siam.org/meetings/an09/
July 20-24, 2009
FPSAC'09-21st Annual International Conference on Formal Power Series and Algebraic Combinatorics, Hagenberg, Austria 15.5 \#3
http://www.risc.jku.at/conferences/fpsac2009
July 20-25, 2009
10th Symposium on Orthogonal Polynomials, Special Functions and Applications (OPSFA-10), Leuven, Belgium
15.5 \#2 16.1 \#2
http://wis.kuleuven.be/OPSFA/OPSFA10.html

## September 4-9, 2009

2nd Dolomites Workshop on Constructive Approximation and Applications" (DWCAA09), Alba di Canazei (Trento), Italy
http://www.math.unipd.it/~dwcaa09
September 13-19, 2009
International Conference on Functional Equations and Inequalities, Krakow, Poland
http://mat.ap.krakow.pl/icfei/13ICFEI/index.php

## September 24-30, 2009

6th Maratea Conference on Functional Analysis and Approximation Theory (FAAT2009), Acquafreda di Maratea, Italy
http://www.dm.uniba.it/faat2009

## Topic \#1 ----------- OP-SF NET 16.2 --------- March 15, 2009

From: OP-SF NET Editors<br>Subject: Ancient Chinese Mathematics

In the January/February 2009 issue of SIAM News Philip Davis wrote a review of Simon Winchester's "The Man Who Loved China". This book describes the life of Joseph Needham, a distinguished biochemist from Cambridge University, England, and author of the multi-volume "Science and Civilization in China" (Cambridge University Press). Volume 3 (1959) contains 168 pages on ancient Chinese mathematics, which is why Needham is a person of particular interest to Davis and to us. The reviewer discusses not just the book under review, but has interesting things to say about the critical reception of Needham's work by later historians of science. For criticisms of Needham specific to mathematics, Davis turns to the book "A History of Chinese Mathematics" by Jean-Claude Martzloff, which, in his outsider's judgment, is currently the best general history of the subject; it places the mathematics strongly within the ancient Chinese cultural context.

Tom Koornwinder wrote the following reaction to Davis' book review as a Letter to the Editor. This reaction will appear in the next issue of SIAM News.

With interest I read Philip Davis's book review "Why Didn't They ...?" in SIAM News (January/February 2009, page 6). Encouraged by his recommendation, I borrowed the book A History of Chinese Mathematics by J.-C. Martzloff from the library. However, I am somewhat disappointed by the coverage of Zhu Shijie (ca. 1300) in this book.

See Needham, Vol. 3, pp. 138, 139 for formulas due to Zhu Shijie (written by Needham as Chu Shih-Chieh), which were reformulated by Askey (Orthogonal Polynomials and Special Functions, SIAM, 1975, pp. 59, 60) as Vandermonde's sum (the explicit summation of the terminating Gauss hypergeometric function of argument 1). Therefore, Vandermonde's sum is now called the Chu-Vandermonde sum by the special functions community.

Martzloff, however, does not mention this work by Zhu Shijie. He does treat in some detail in Chapter 18 the much later (19th century) work of Li Shanlan. The formula (18.1) there can be reformulated as a special case of Saalschutz's formula for hypergeometric ${ }_{3} F_{2}(1)$. According to secondary sources quoted by Askey, this formula (18.1), too, seems to go back to Zhu Shijie. However, the only mention of Zhu Shijie in Chapter 18 is in a quote from the preface of the book by Li Shanlan:
"Master Zhu Shijie from the Yuan dynasty is the only one who has made use of the prescriptions relating the piling up of heaps in the chapters of his Siyuan yujian entitled ... . But his intention was only to expound the algebra and for that reason he presents the piling up of heaps neither precisely nor methodically."

Martzloff speculates in this chapter about influences on Li Shanlan by Western mathematical work. But if some of Li Shanlan's formulas go back to Zhu Shijie, then Western influence on this part is less probable.

Needham, after the formulas quoted by Askey, hints at "many other formulas of similar nature" given by Chu Shih-Chieh. I would like to see a transcription of this part of Chu's writings, to learn what further treasures his work might contain.

Tom Koornwinder,
Korteweg-de Vries Institute for Mathematics, University of Amsterdam.

## Topic \#2 ---------- OP-SF NET 16.2 --------- March 15, 2009

From: OP-SF NET Editors
Subject: Preprints in arXiv.org
The following preprints related to the fields of orthogonal polynomials and special functions were posted or cross-listed to one of the subcategories of arXiv.org mostly during January and February 2009.
http://arxiv.org/abs/0901.0054
Counting decomposable univariate polynomials
Authors: Joachim von zur Gathen
http://arxiv.org/abs/0901.0190
Airy functions over local fields
Authors: Rahul N. Fernandez, V. S. Varadarajan, David Weisbart
http://arxiv.org/abs/0901.0249
On the q-Extensions of the Bernoulli and Euler Numbers, Related Identities and Lerch Zeta Function
Authors: Taekyun Kim, Younghee Kim, kyoungwon Hwang
http://arxiv.org/abs/0901.0324
Beta Jacobi processes
Authors: Nizar Demni
http://arxiv.org/abs/0901.0353
New approach to q-Genocch, Euler numbers and polynomials and their interpolation functions
Authors: Taekyun Kim
http://arxiv.org/abs/0901.0435
Convergence of ray sequences of Pade approximants to 2 F1 ( $\mathrm{a}, 1 ; \mathrm{c} ; \mathrm{z}$ ), c>a>0
Authors: K Driver, K Jordaan
http://arxiv.org/abs/0901.0746
$\mathrm{O}(\mathrm{N})$ colour-flavour transformations and characteristic polynomials of real random matrices
Authors: Yi Wei, Boris A. Khoruzhenko
http://arxiv.org/abs/0901.0837
Structural Relations of Harmonic Sums and Mellin Transforms at Weight w=6 Authors: Johannes Blümlein
http://arxiv.org/abs/0901.0897
Gap Probabilities in Non-Hermitian Random Matrix Theory
Authors: G. Akemann, M.J. Phillips, L. Shifrin
http://arxiv.org/abs/0901.0947
Orthogonal polynomials on the unit circle, \$q\$-Gamma weights, and discrete Painlevé equations
Authors: Philippe Biane
http://arxiv.org/abs/0901.0982
Complex Hadamard matrices from Sylvester inverse orthogonal matrices
Authors: Petre Dita
http://arxiv.org/abs/0901.1104
Mathieu's series: inequalities, asymptotics and positive definiteness
Authors: Viktor P. Zastavnyi
http://arxiv.org/abs/0901.1379
Pseudo-factorials, elliptic functions, and continued fractions
Authors: Roland Bacher, Philippe Flajolet
http://arxiv.org/abs/0901.1548
On Gram's law in the theory of the Riemann zeta function
Authors: Jan Mozer
http://arxiv.org/abs/0901.1697
Note on the generalization of the higher order q-Genocchi numbers and q-Euler numbers
Authors: Taekyun Kim, Young-hee Kim, Kyoung-won Hwang
http://arxiv.org/abs/0901.1725
Inequalities for the eigenvalues of non-selfadjoint Jacobi operators
Authors: Marcel Hansmann, Guy Katriel
http://arxiv.org/abs/0901.1883
Hankel determinants of Dirichlet series
Authors: H. Monien
http://arxiv.org/abs/0901.2006
The fermionic $p$-adic integrals on $Z p$ associated with extended $q$-Euler numbers and polynomials
Authors: Taekyun Kim
http://arxiv.org/abs/0901.2083
Some applications of the Stieltjes constants
Authors: Donal F. Connon
http://arxiv.org/abs/0901.2424
A new type of critical behaviour in random matrix models
Authors: R. Flume, A. Klitz
http://arxiv.org/abs/0901.2473
Higher order analogues of the Tracy-Widom distribution and the Painleve II
hierarchy
Authors: T. Claeys, A. Its, I. Krasovsky
http://arxiv.org/abs/0901.2655
On Non-central Stirling Numbers of the First Kind
Authors: Milan Janjic
http://arxiv.org/abs/0901.2940
Orthogonality of Jacobi and Laguerre polynomials for general parameters via the Hadamard finite part
Authors: Rodica D. Costin
http://arxiv.org/abs/0901.3328
On the Geometric Interpretation of the Complex Fourier Transforms of a Class of Exponential Functions
Authors: Jeremy Williams
http://arxiv.org/abs/0901.3377
Mean Staircase of the Riemann Zeros: a comment on the Lambert W function and an algebraic aspect
Authors: Davide a Marca, Stefano Beltraminelli, Danilo Merlini
http://arxiv.org/abs/0901.3379
Zonal polynomials and hypergeometric functions of quaternion matrix argument Authors: Fei Li, Yifeng Xue
http://arxiv.org/abs/0901.3452
Ramanujan Summation and the Exponential Generating Function \$
\sum_\{k=0\}^\{\infty\}\frac\{z^\{k\}\}\{k!\}\zeta $\wedge\{\backslash$ prime $\}(-k) \$$
Authors: B. Candelpergher, H. Gopalkrishna Gadiyar, R. Padma
http://arxiv.org/abs/0901.3518
On the Zeros of the Complex Fourier Transforms of a Class of Exponential Functions
Authors: Jeremy Williams
http://arxiv.org/abs/0901.3970
Integrals of products of Hermite functions
Authors: Wei-Min Wang
http://arxiv.org/abs/0901.3973
Jacob's ladders and the almost exact asymptotic representation of the Hardy-
Littlewood integral
Authors: Jan Moser
http://arxiv.org/abs/0901.4176
The sl_3 Selberg integral
Authors: S. Ole Warnaar
http://arxiv.org/abs/0901.4501
Some properties of deformed \$q\$-numbers
Authors: Thierry C. Petit Lobão, Pedro G. S. Cardoso, Suani T. R. Pinho, Ernesto
P. Borges
http://arxiv.org/abs/0901.4564
The p -adic valuations of sequences counting alternating sign matrices Authors: Xinyu Sun, Victor H. Moll
http://arxiv.org/abs/0901.4680
Hankel determinants of Schroeder-like numbers
Authors: Johann Cigler
http://arxiv.org/abs/0901.4698
Hankel determinants of q-exponential polynomials
Authors: Johann Cigler
http://arxiv.org/abs/0901.2244
Matrix valued Szego polynomials and quantum random walks
Authors: M. J. Cantero, F. A. Grünbaum, L. Moral, L. Velazquez
http://arxiv.org/abs/0901.2717
On the Spatial Asymptotics of Solutions of the Toda Lattice
Authors: Gerald Teschl
http://arxiv.org/abs/0901.4716
Feynman Diagrams, Differential Reduction, and Hypergeometric Functions
Authors: M. Yu. Kalmykov (Hamburg U., Inst. Theor. Phys. II \& Dubna, JINR), V. V. Bytev (Hamburg U., Inst. Theor. Phys. II \& Dubna, JINR) Bernd A. Kniehl (Hamburg U., Inst. Theor. Phys. II), B.F.L. Ward (Baylor U.), S.A. Yost (Citadel Military Coll.)
http://arxiv.org/abs/0902.0041
Polynomial solutions of differential-difference equations
Authors: Diego Dominici, Kathy Driver, Kerstin Jordaan
http://arxiv.org/abs/0902.0051
Compatibility of the Theta correspondence with the Whittaker functors
Authors: Vincent Lafforgue (University Paris 6), Sergey Lysenko (University Nancy 1)
http://arxiv.org/abs/0902.0054
On generalized Cauchy-Stieltjes transforms of some Beta distributions
Authors: Nizar Demni
http://arxiv.org/abs/0902.0116
A passage to the Poisson-Dirichlet through the Bessel square processes
Authors: Soumik Pal
http://arxiv.org/abs/0902.0193
Critical measures, quadratic differentials, and weak limits of zeros of Stieltjes polynomials
Authors: A. Martinez-Finkelshtein, E. A. Rakhmanov
http://arxiv.org/abs/0902.0380
Special Functions Related to Dedekind Type DC-Sums and their Applications Authors: Yilmaz Simsek
http://arxiv.org/abs/0902.0413
On the number of real critical points of logarithmic derivatives and the Hawaii conjecture
Authors: Mikhail Tyaglov
http://arxiv.org/abs/0902.0451
Cariñena polynomials are Jacobi polynomials
Authors: C. Vignat, P.W. Lamberti
http://arxiv.org/abs/0902.0621
Basic hypergeometric functions as limits of elliptic hypergeometric functions
Authors: Fokko van de Bult, Eric Rains
http://arxiv.org/abs/0902.0789
The series limit of sum_k 1/[k log k (log $\log k) \wedge 2]$
Authors: Richard J. Mathar
http://arxiv.org/abs/0902.0797
De Toda à KdV
Authors: Dario Bambusi, Thomas Kappeler, Thierry Paul (DMA)
http://arxiv.org/abs/0902.0804
On a nonlinear recurrent relation
Authors: Dong Li
http://arxiv.org/abs/0902.0852
Computing the smallest eigenvalue of large ill-conditioned Hankel matrices
Authors: Niall Emmart, Charles C. Weems, Yang Chen
http://arxiv.org/abs/0902.0910
A novel analytical operator method to solve linear ordinary differential equations with variable coefficients
Authors: Wrick Sengupta
http://arxiv.org/abs/0902.1027
Condensation of the roots of real random polynomials on the real axis
Authors: Gregory Schehr, Satya N. Majumdar
http://arxiv.org/abs/0902.1058
Multiple orthogonal polynomial ensembles
Authors: Arno B.J. Kuijlaars
http://arxiv.org/abs/0902.1650
A simple approach to some Hankel determinants
Authors: Johann Cigler
http://arxiv.org/abs/0902.1691
A recurrence relation for the Li/Keiper constants in terms of the Stieltjes constants
Authors: Donal F. Connon
http://arxiv.org/abs/0902.2099
Recurrence formulas for Macdonald polynomials of type A
Authors: Michel Lassalle, Michael J. Schlosser
http://arxiv.org/abs/0902.2188
Some integrals involving the Stieltjes constants
Authors: Donal F. Connon
http://arxiv.org/abs/0902.2390
Group Classification of a family of second-order differential equations
Authors: J.C. Ndogmo
http://arxiv.org/abs/0902.2513
A complete solution to an open problem relating to an inequality for ratios of gamma functions
Authors: Feng Qi, Bai-Ni Guo
http://arxiv.org/abs/0902.2514
Bounds for the ratio of two gamma functions--From Wendel's limit to Elezović-Giordano-Pečarić's theorem
Authors: Feng Qi
http://arxiv.org/abs/0902.2519
A short proof of monotonicity of a function involving the psi and exponential functions
Authors: Feng Qi, Bai-Ni Guo
http://arxiv.org/abs/0902.2588
Concise sharpening and generalizations of Shafer's inequality for the arc sine function
Authors: Feng Qi, Bai-Ni Guo
http://arxiv.org/abs/0902.2991
Generalized Heun and Lamé's equations: factorization
Authors: Mahouton Norbert Hounkonnou, André Ronveaux
http://arxiv.org/abs/0902.3073
Log-convexity and log-concavity of hypergeometric-like functions
Authors: D.Karp, S.M. Sitnik
http://arxiv.org/abs/0902.3190
On a polynomial zeta function
Authors: Sergio L. Cacciatori
http://arxiv.org/abs/0902.3440
Curves defined by Chebyshev polynomials
Authors: Gene Freudenburg, Jenna Freudenburg
http://arxiv.org/abs/0902.3870
Asymptotic Independence of the Extreme Eigenvalues of GUE
Authors: Folkmar Bornemann
http://arxiv.org/abs/0902.3953
Nearest lambda_q-multiple fractions
Authors: Dieter Mayer, Tobias Mühlenbruch
http://arxiv.org/abs/0902.4064
Differential equations for deformed Laguerre polynomials
Authors: Peter J. Forrester, Christopher M. Ormerod
http://arxiv.org/abs/0902.4169
Arithmetic theory of q-difference equations (G_q-functions and q-difference modules of type G, global q-Gevrey series)
Authors: Lucia Di Vizio
http://arxiv.org/abs/0902.4608
Quantum alpha-determinants and q-deformed hypergeometric polynomials
Authors: Kazufumi Kimoto
http://arxiv.org/abs/0902.4732
On the number zeta(3)
Authors: L.A.Gutnik
http://arxiv.org/abs/0902.1974
Coherent states of a particle in magnetic field and Stieltjes moment problem Authors: J.P. Gazeau, M.C. Baldiotti, D.M. Gitman

## Topic \#3 ---------- OP-SF NET 16.2 --------- March 15, 2009

From: OP-SF NET Editors
Subject: About the Activity Group
The SIAM Activity Group on Orthogonal Polynomials and Special Functions consists of a broad set of mathematicians, both pure and applied. The Group also includes engineers and scientists, students as well as experts. We have around 140 members scattered about in more than 20 countries. Whatever your specialty might be, we welcome your participation in this classical, and yet modern, topic. Our WWW home page is:
http://math.nist.gov/opsf/
This is a convenient point of entry to all the services provided by the Group. Our Webmaster is Bonita Saunders (bonita.saunders@nist.gov).

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http://www.mathematik.uni-kassel.de/~koepf/siam.html
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Finally, the Activity Group operates an email discussion group, called OP-SF Talk. To subscribe, send the email message
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http://math.nist.gov/opsftalk/archive

## Topic \#4 ----------- OP-SF NET 16.2 --------- March 15, 2009

From: OP-SF NET Editors
Subject: Submitting contributions to OP-SF NET
To contribute a news item to OP-SF NET, send email to poly@siam.org with a copy to one of the OP-SF Editors dominicd@newpaltz.edu or muldoon@yorku.ca. Contributions to OP-SF NET 16.3 should be sent by May 1, 2009.

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The elected Officers of the Activity Group (2008-2010) are:
Francisco J. Marcellán, Chair
Peter A. Clarkson, Vice Chair
Daniel W. Lozier, Secretary
Peter A. McCoy, Program Director
The appointed officers are:
Diego Dominici, OP-SF NET co-editor Martin Muldoon, OP-SF NET co-editor Bonita Saunders, Webmaster

