

# OP-SF NET – Volume 30, Number 4 – July 15, 2023

The Electronic News Net of the  
SIAM Activity Group on Orthogonal Polynomials and Special Functions

<http://math.nist.gov/opsf>

OP-SF Net is distributed to OPSF Activity Group members and non-members alike through the OP-SF Talk listserv.

If you are interested in subscribing to the Newsletter and/or OP-SF Talk, or if you would like to submit a topic to the Newsletter or a contribution to OP-SF Talk, please send an email to the OP-SF Net Editors.

Editors:

Howard S. Cohl  
Sarah Post

[howard.cohl@nist.gov](mailto:howard.cohl@nist.gov)  
[spost@hawaii.edu](mailto:spost@hawaii.edu)

Topics:

1. Report by **Van Assche**: AAA2023, **Gradimir Milovanović** 75<sup>th</sup> in Vrnjačka Banja, Serbia
2. Report by: **Van der Jeugt**: Algebraic structures and SF, **Luc Vinet** 70<sup>th</sup> in Ghent, Belgium
3. Report by: **Kuijlaars**: OP & Applications, dedicated to **Walter Van Assche** in Leuven, Belgium
4. Report by: **Organizers**: ILAS2023: Minisymposium on OP & Matrix Analysis in Madrid, Spain
5. Report by: **Martínez-Finkelshtein**: FoCM 2023 conference & OPSF Workshop in Paris, France
6. Report by: **Dumitriu**: FoCM 2023 conference, Workshop on Random Matrices in Paris, France
7. Preprints in arXiv.org
8. Submitting contributions to OP-SF NET and SIAM-OPSF (OP-SF Talk)
9. Thought of the Month by **Tom H. Koornwinder**

## Calendar of Events:

### August 14–18, 2023

International Conference on Spectral Theory and Approximation ([ICSTA](#))  
Lund University, Lund, Sweden.

<https://icsta.se/>

\* Registration is now open (deadline June 14)

\* Funding is available for Ph.D. students/postdocs

### December 14–15, 2023

4th Workshop “Two Days of Orthogonal Polynomials ”

University of Almería, Almería, Spain

Dedicated to Guillermo López Lagomasino for his 75th anniversary and to  
Andrei Martínez Finkelshtein for his 60th anniversary.

<https://w3.ual.es/GruposInv/Tapo/D2PO-2023/comollegar.html>

## January 3–6, 2024

2024 [Joint Mathematics Meetings](https://www.jointmathematicsmeetings.org/meetings/national/jmm2024/2300_program.html), American Mathematical Society,  
Moscone Center, San Francisco, California, USA

[https://www.jointmathematicsmeetings.org/meetings/national/jmm2024/2300\\_program.html](https://www.jointmathematicsmeetings.org/meetings/national/jmm2024/2300_program.html)

AWM–AMS Noether Lecture: Anne Schilling: [The Ubiquity of Crystal Bases](#)

AMS Special Session on Numerical Analysis, Spectral Graph Theory, Orthogonal Polynomials,  
and Quantum Algorithms,

Organized by Anastasiia Minenkova, Gamal Mograby, and Anastasiia Minenkova (SS 92A)

AMS Special Session on Partition Theory and  $q$ -Series,

Organized by William Jonathan Keith, Brandt Kronholm, and Dennis Eichhorn (SS 30A)

## June 24–28, 2024

17<sup>th</sup> International Symposium on Orthogonal Polynomials, Special Functions and Applications  
(OPSFA–17),

Universidad de Granada, Granada, Spain.

<https://opsfa17.com/>

## Topic #1 ——— OP – SF Net 30.4 ——— July 15, 2023

From: Walter Van Assche ([walter.vanassche@kuleuven.be](mailto:walter.vanassche@kuleuven.be))

Subject: Report by **Van Assche**: AAA2023, **Gradimir Milovanović** 75<sup>th</sup> in Vrnjačka Banja, Serbia

Report on *International Mathematical Conference on Analysis, Approximation and Applications* (AAA2023)  
by Walter Van Assche

In order to celebrate the 75<sup>th</sup> birthday of Professor Gradimir Milovanović, an international conference was held in Vrnjačka Banja, a popular spa in Serbia, some 200 km south of Belgrade, from July 21 to July 24, 2023. There were four plenary talks by Alexander Aptekarev, Vilmos Totik, Paco Marcellán and Walter Van Assche on topics close to the research interests of Milovanović, i.e.,  $L^p$ -bounds for orthogonal polynomials, polynomial inequalities, orthogonal polynomials and quadrature formulas, and multiple orthogonal polynomials. On the first day, Miodrag Spalević and Marija Stanić gave an overview of the life and scientific career of Gradimir Milovanović, who was a professor at the University of Niš from 1986 to 2008, where he was Rector from 2004 until 2006, and from 2008 to 2011, he was Dean of the Faculty of Computer Sciences at Megatrend University. At present he is a Research Professor at the Mathematical Institute of the Serbian Academy of Sciences and Arts (SANU) and he is a full member of the Serbian Academy since 2012.

There was also a talk by Walter Gautschi, a special guest and longtime collaborator of Milovanović, who proved that at the age of 95 one can still do interesting and relevant mathematical research by presenting his work on Gauss quadrature for Ramanujan's integral

$$\int_0^1 \frac{\Gamma(a, t)}{\Gamma(a)} da,$$

which involves the gamma function and the incomplete gamma function. The contributed talks were in three parallel sessions. All the talks took place in a local Gymnasium (high school) at Vrnjačka Banja.



Figure 1: Group photo with Gradimir Milovanović on the first row, third from the right, next to Walter Gautschi and Marija Stanić.

Topic #2 ——— OP – SF Net 30.4 ——— July 15, 2023

From: Joris Van der Jeugt ([Joris.VanderJeugt@ugent.be](mailto:Joris.VanderJeugt@ugent.be))

Subject: Report by: **Van der Jeugt**: Algebraic structures and SF, **Luc Vinet** 70<sup>th</sup> in Ghent, Belgium

Report on the Workshop “[Algebraic structures and special functions in theoretical physics](#)”, Ghent, Belgium, 26–30 June 2023.

This workshop was organized to celebrate the achievements of Professor Luc Vinet (Montreal) on the occasion of his 70<sup>th</sup> birthday. The aim of this workshop, where participation was by invitation only, was to bring together researchers and scientists who have collaborated with Luc or whose work is close to that of Luc. The organizers (Hendrik De Bie and Joris Van der Jeugt from Ghent University, and Nicolas Crampé from University of Tours) had a limited budget available, so it was not possible to invite all scientists of the huge network of Luc. So they had to make a choice, based on availability and on personal contacts. Senior scientists as well as young postdocs from Luc were present.

Luc Vinet is a leading figure in the field of mathematical physics. He is known for his expertise in: algebraic structures, special functions and orthogonal polynomials, theory of quantized fields, quantum information, quantum mechanics, symmetry and conservation laws, integrable systems and random processes. All of these areas were covered during the workshop. Quite a lot of presentations were on

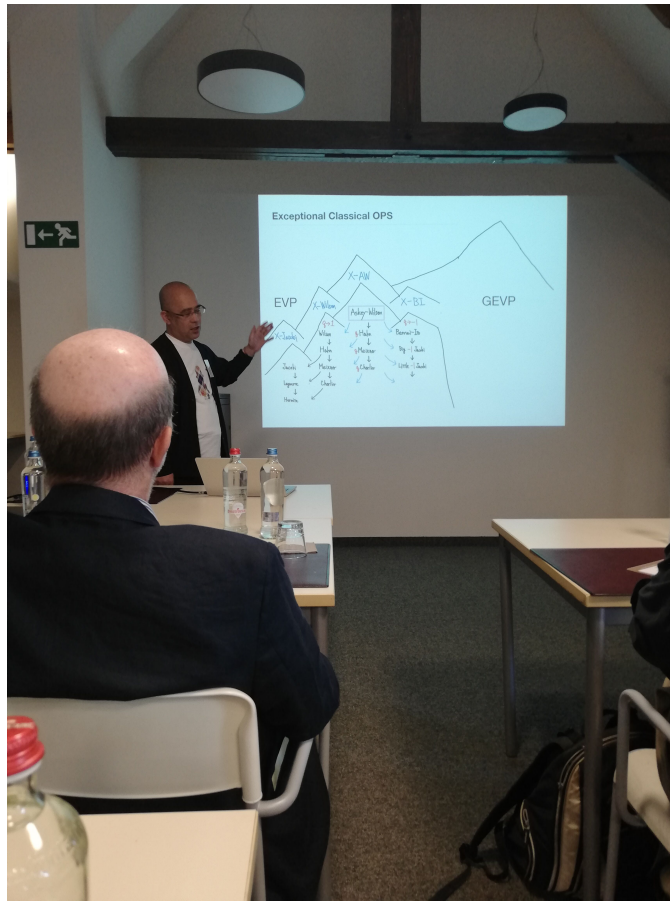


Figure 2: Satoshi Tsujimoto explains his extension of the Askey mountains. Photo provided by Hendrik De Bie.

topics of relevance for this SIAM Activity Group. To name a few: Luc Lapointe talked about  $m$ -symmetric Macdonald polynomials; Luc Frappat about multivariate orthogonal polynomials in a icosidodecahedron scheme, derived from the rank two Racah algebra; Plamen Iliev about the Gaudin model for the multinomial distribution; Tom Koornwinder about symmetric and nonsymmetric Askey–Wilson functions and symmetries of the Askey–Wilson DAHA; Eric Koelink about convolution identities; Julien Gaboriaud about tridiagonal pairs of particular shape, the  $sl(2)$  algebra and underlying orthogonal polynomials; Walter Van Assche about multiple orthogonal polynomials; Loïc Poulain d’Andecy about Racah polynomials and Rankin–Cohen brackets; Satoshi Tsujimoto about exceptional biorthogonal rational functions.

Yvan Saint–Aubin presented, apart from a scientific talk, also a special presentation on the Life(s) of Luc, and the different highlights as a scientist, as an organizer, as a director and manager, as a leader, promoter and supervisor who always brings out the best in his students and postdocs.

All participants stayed in the same hotel [Monasterium Poortackere](#), in the historic center of Ghent, where the workshop itself took place in a conference room. There were long breaks, so participants had time to exchange ideas and to get inspiration for future work. The participants and Luc enjoyed the charming place, the beautiful surroundings, and the relaxed atmosphere of the workshop.



Figure 3: Yvan Saint-Aubin presenting the life(s) of Luc. Photo provided by Hendrik De Bie.



Figure 4: Conference dinner ‘honorary’ table: Back row: Hendrik De Bie – Luc Vinet – Letitia (wife of Luc) – Nicolas Crampé. Front row: Hendrik’s wife Annelies – Joris’s wife Vera – Joris Van der Jeugt – Jean-Sébastien Caux. Photo provided by Hendrik De Bie.

From: Arno Kuijlaars ([arno.kuijlaars@kuleuven.be](mailto:arno.kuijlaars@kuleuven.be))

Subject: Report by: **Kuijlaars**: OP & Applications, dedicated to **Walter Van Assche** in Leuven, Belgium

Report on: *Orthogonal Polynomials and Applications*, June 8–10, 2023, in Leuven, Belgium, a conference dedicated to **Walter Van Assche**.

**Walter Van Assche** is a leading figure in the field of orthogonal polynomials, special functions and their applications. He made fundamental contributions to orthogonal and multiple orthogonal polynomials, their algebraic and analytic properties as well as to their asymptotic analysis.



Figure 5: The grave of Stieltjes in Toulouse (taken in March 1995) together with Jacob Korevaar (who turned 100 this year) and Marcel de Bruin.

With the conference in Leuven, we celebrated the achievements of Walter Van Assche on the occasion of his 65<sup>th</sup> birthday. In the Belgian situation, reaching the age of 65 inevitably means that Walter will be emeritus professor, starting October 1<sup>st</sup>, 2023. However, he promised to remain active in research.

The conference was attended by around 50 participants, many old friends and colleagues of Walter, but also younger researchers. The program consisted of 9 invited talks and 17 shorter contributions. The talks gave a good overview of current developments in orthogonal polynomials and special functions.

Interesting contributions from Ph.D. students and postdocs showed that the field continues to attract new young people. The talks were met with lively discussions.

Alexander Aptekarev, Galina Filipuk, and Paul Nevai, who were not able to join the meeting in person, gave their online greetings to Walter. They joined the other participants in showing pictures of Walter at various events, and sharing their reminiscences about more than 40 successful years of work in orthogonal polynomials and special functions.



Figure 6: Two giants in OPSFA: Askey and Olver, taken in Washington DC in April 2011.

At the end of the conference, also Walter contributed by showing his own set of pictures. This included many of the friends and colleagues that were present at this memorable event.

Topic #4 ——— OP – SF Net 30.4 ——— July 15, 2023

From: Paco Marcellán ([pacomarc@ing.uc3m.es](mailto:pacomarc@ing.uc3m.es)), Amilcar Branquinho ([ajplb@mat.uc.pt](mailto:ajplb@mat.uc.pt)),  
Ana Foulquié ([foulquie@ua.pt](mailto:foulquie@ua.pt)), Manuel Mañas ([mmanasba@ucm.es](mailto:mmanasba@ucm.es))

Subject: Report by: **Organizers**: ILAS2023: Minisymposium on OP & Matrix Analysis in Madrid, Spain

The contributed Minisymposium on Orthogonal Polynomials, Matrix Analysis and Applications at the 25<sup>th</sup> Conference of the International Linear Algebra Society (ILAS2023), which took place in Madrid, Spain, on June 14–16, 2023, was dedicated to discussing recent trends in the field of orthogonal polynomials, matrix analysis, and their applications in various areas. The event was held in the historical

buildings of the Polytechnic School for Forestry, Forest Engineering, and Natural Environment, Universidad Politécnica de Madrid, creating a friendly atmosphere. Over the course of three days, we had 13 talks, each lasting half an hour, with an average audience size of 30 people per talk.

During the first session on Wednesday morning, Jean Bernard Lasserre (Université de Toulouse, France) presented a talk on the applications of the Christoffel function in real algebraic geometry, the equilibrium measure of compact sets, polynomial Pell's equation, and duality in polynomial optimization. Teresa E. Pérez (Universidad de Granada, Spain) introduced a time-dependent parameter and explained how to solve a Lax-type pair system for the coefficients of the three-term relations. She also deduced several characterizations relating the Lax-type pair, the shape of the weight, Stieltjes function, moments, a differential equation for the weight, and bidimensional Toda-type systems. Maxim Derevyagin (University of Connecticut, USA) reviewed the basics of discrete Darboux transformations for orthogonal polynomials, demonstrating how these transformations lead to various types of orthogonalities such as Sobolev and exceptional, and how they generate rational orthogonal functions. Francisco Marcellán (Universidad Carlos III de Madrid, Spain) discussed Darboux transformations for CMV matrices and the presence of spurious solutions, illustrating that these spurious solutions are associated with certain Sobolev inner products.

The Thursday morning session featured talks on bivariate orthogonality, exceptional orthogonality, and Sobolev orthogonal polynomials, delivered by Jeffrey S. Geronimo (Georgia Institute of Technology, USA), Mirta M. Castro Smirnova (Universidad de Sevilla, Spain), and Niel van Buggenhout (Univerzita Karlova, Czech Republic), respectively. Jeff presented a class of Bernstein-Szegő measures on  $\mathbb{R}^2$ , extending the one-dimensional class of Bernstein-Szegő measures, and discussed their spectral properties as well as conditions involving finitely many moments that completely characterize this class. Mirta discussed examples of exceptional orthogonal polynomials in connection with the problem of time and band-limiting. Niel introduced the projection of a certain Jordan matrix onto the Krylov subspace to obtain a Hessenberg matrix containing the recurrence coefficients for polynomials orthogonal with respect to a Sobolev inner product. He proposed two new algebraic methods for the numerical generation of Sobolev orthogonal polynomials and compared them to existing methods.

In the afternoon, Ana Foulquié Moreno (Universidade de Aveiro, Portugal) and Vladimir Lysov (Keldysh Institute of Applied Mathematics, Russia) presented talks on recursion matrices and multiple orthogonal polynomials. Raquel Gonzalo (Universidad Politécnica de Madrid, Spain) focused her presentation on Sobolev orthogonality. Ana showed how the spectral and factorization properties of oscillatory matrices lead to a spectral Favard theorem for bounded banded matrices that admit a positive bidiagonal factorization, in terms of sequences of mixed multiple orthogonal polynomials with respect to a set of positive Lebesgue-Stieltjes measures. She also proved a mixed multiple Gauss quadrature and determined the corresponding degrees of precision. Vladimir considered tridiagonal Jacobi matrices (or discrete Schrödinger operators) on graphs, implementing such operators on homogeneous trees using Hermite-Padé interpolation problems for perfect systems. He posed an interpolation problem for Nikishin systems, a subclass of perfect systems, in which the solutions satisfy nearest-neighbor recurrent relations while the coefficients and the Jacobi matrix remain bounded. Finally, Raquel discussed the problem of locating the zeros of Sobolev polynomials associated with compactly supported measures in the complex plane, applying a matrix analysis approach through the associated moment matrix.

The final session, held on Friday morning, included three talks on matrix analysis in moment problems and orthogonal polynomial theory, presented by Alberto Lastra (Universidad de Alcalá, Spain), Luis Verde-Star (Universidad Autónoma Metropolitana, Mexico), and Carmen Escribano (Universidad Politécnica de Madrid, Spain). Alberto considered kernel functions for generalized summability to find the general solution to a linear system of moment differential equations  $\partial_m y = Ay$  for a given complex matrix  $A$ . He illustrated this method with different sequences  $m$ , describing the asymptotic growth of the solutions at infinity in terms of the associated moment sequence from various perspectives. Luis showed that the three-term recurrence relation satisfied by a sequence of orthogonal polynomials can be expressed as the matrix equation  $LC = CX$ , where  $L$  is the infinite tridiagonal Jacobi matrix with



recurrence coefficients,  $C$  is a given matrix, and  $X$  is the right shift matrix representing the operator of multiplication by  $x$ . This matrix equation was used to obtain simple algebraic formulas for the linearization coefficients. Finally, Carmen discussed Sobolev orthogonal polynomials using matrix analysis via the associated moment matrix. She focused on the behavior of eigenvalues of Hermitian positive definite matrices associated with inner Sobolev products with respect to a set of measures, in relation to the problem of locating zeros of Sobolev orthogonal polynomials. She provided results in this context.

Organizers: **Amilcar Branquinho, Ana Foulquié, Manuel Mañas and Francisco Marcellán**

Topic #5 ——— OP – SF Net 30.4 ——— July 15, 2023

From: Andrei Martínez–Finkelshtein ([andrei@ual.es](mailto:andrei@ual.es))

Subject: Report by: **Martínez–Finkelshtein**: FoCM 2023 conference & OPSF Workshop in Paris, France

Report on Workshop on Special Functions and Orthogonal Polynomials, Session III.7 of [FoCM 2023](#), June 19–21, 2023, Paris, France, by Andrei Martínez–Finkelshtein.



Figure 7: Some participants of the FoCM 2023 workshop “Special Functions and Orthogonal Polynomials”. Photo taken by Andrei Martínez–Finkelshtein.

The 2023 Foundations of Computational Mathematics (FoCM 2023) conference that took place in Paris in June was the ninth conference of the FoCM society, following the meeting that gave birth to the idea of FoCM in Park City (1995) and eight very successful meetings in Rio de Janeiro (1997), Oxford (1999), Minneapolis (2002), Santander (2005), Hong Kong (2008), Budapest (2011), Montevideo (2014) and Barcelona (2017). The conference in Vancouver planned for 2020 was canceled due to the Covid-19 pandemic. These conferences typically attract hundreds of participants from all branches of mathematics, and this one was no exception.

As usual, the conference was organized in three periods, with plenary talks in the mornings and workshops (including poster sessions) in the afternoons running in parallel. Among other highlights, Walter Van Assche gave a plenary talk about multiple orthogonal polynomials, and the 2023 Vasil A. Popov prize winner was announced (Matthew Colbrook, from the University of Cambridge).

The third period (June 19–21) had the workshop “Special Functions and Orthogonal Polynomials,” organized by Ana Loureiro, Paco Marcellán, and Andrei Martínez–Finkelshtein. There were 18 talks, among them three semi-plenary (Peter Clarkson, Rob Milson, and Dan Huybrechs), and 10 poster contributors. All sessions took place at the Sorbonne University International Conference Center in central Paris.

## Topic #6 ——— OP – SF Net 30.4 ——— July 15, 2023

From: Ioana Dumitriu ([idumitriu@ucsd.edu](mailto:idumitriu@ucsd.edu))

Subject: Report by: **Dumitriu**: FoCM 2023 conference, Workshop on Random Matrices in Paris, France

Report on Workshop on Random Matrices, Session II.5 of [FoCM 2023](#), June 15–17, 2023, Paris, France, by Ioana Dumitriu.

This workshop was part of the Foundations of Computational Mathematics 2023 conference, which took place during June 12–21 in Paris, at the Sorbonne University; our workshop took place during the second period (June 15–17). By design, FoCM conferences consist of plenary talks in the mornings and workshops in the afternoon. Over the course of the three afternoons of the workshop, we listened to 14 talks by a variety of researchers; the workshop also contributed three poster submissions to the conference poster session for Period II.

The aim of the workshop was twofold: one, to highlight new developments in random matrix theory and two, to showcase new and interesting uses of random matrix theory in other fields, from randomized numerical linear algebra to statistical physics, quantum computation, combinatorics, and data science. We had two semi-plenary talks, by Gunnar Martinsson (UT Austin) on June 16, and by Roman Vershynin (UC Irvine) on June 17. Gunnar’s talk was a survey of techniques for producing low-rank approximations for matrices, including state-of-the-art algorithms; Roman presented a (new) weak Szemerédi regularity lemma using Grothendieck’s identity; both of these talks fit under the second objective of our workshop (applications).

The workshop included presentation on theoretical random matrix theory results, with talks on June 15 by Ke Wang (HKUST) on random perturbations of low-rank matrices and by Alan Edelman (MIT) on the conditional determinantal point processes (DPP) approach to random matrix distributions. On June 16, we were treated to an unscheduled talk by March Boedihardjo (Michigan State University) on the spectral radii of symmetric inhomogeneous random matrices and a presentation by Arno Kuijlaars (Katholieke Universiteit Leuven) on Ginibre ensembles with point insertions; the day was closed by Ioana Dumitriu (UC San Diego) with a talk on the extreme singular values of sparse, rectangular, inhomogeneous matrices.

In addition to the plenary talks, the applications part of the workshop consisted of talks on June 15 by Jorge Garza–Vargas (Caltech) on spectral stability under random perturbations, by Tom Trogdon on the predictability and universality in numerical computation, and by Joel Tropp (Caltech) on using random sparse Hamiltonians to prove quantum advantage. On June 16, Liza Rebrova (Princeton) presented a randomized Kaczmarz method for corrupted linear systems, and Folkmar Bornemann (TU Munich) showcased a method to compute asymptotic expansions relating to the longest increasing subsequences in random permutations. On June 17, Pierre Youssef (NYU Abu Dhabi) presented a surprising method to improve the constant connected to the relaxation time of a Markov chain, and Sheehan Olver (Imperial College) discussed numerical methods for computing equilibrium measures from random matrix theory

as well as extensions to other types of particle interactions.

The poster submissions by Henri Goulart (Toulouse INP / IRIT), Jaehee Kim (Duksung University) and Ryan Schneider (UC San Diego) covered applications to random tensors, brain temporal networks, respectively, randomized computation of generalized eigenvalues. The posters were on display for the duration of the period (June 15–17).

The workshop was well-attended, with audiences reaching into the sixties during the semi-plenary talks, and there was a very good amount of interaction between participants during coffee breaks and also after hours.

Topic #7 ——— OP – SF Net 30.4 ——— July 15, 2023

From: OP–SF Net Editors

Subject: Preprints in arXiv.org

The following preprints related to the fields of orthogonal polynomials and special functions were posted or cross-listed to one of the subcategories of arXiv.org during May and June 2023. This list has been separated into two categories.

### OP–SF Net Subscriber E–Prints

<http://arxiv.org/abs/2305.00791>

Wave functions for quantum integrable particle systems via partial confluences of multivariate hypergeometric functions

Jan Felipe van Diejen, Erdal Emsiz

<http://arxiv.org/abs/2305.00505>

Fixed-time safe tracking control of uncertain high-order nonlinear pure-feedback systems via unified transformation functions

Chaoqun Guo, Jiangping Hu, Jiasheng Hao, Sergej Celikovsky, Xiaoming Hu

<http://arxiv.org/abs/2305.00778>

Symmetry groups, fundamental solutions and conservation laws for conformable time fractional partial differential system with variable coefficients

Xiaoyu Cheng, Lizhen Wang

<http://arxiv.org/abs/2305.01282>

Cubature rules from Hall–Littlewood polynomials

Jan Felipe van Diejen, Erdal Emsiz

<http://arxiv.org/abs/2305.01289>

Cubature rules for unitary Jacobi ensembles

Jan Felipe van Diejen, Erdal Emsiz

<http://arxiv.org/abs/2305.01532>

Maximal polarization for periodic configurations on the real line

Markus Faulhuber, Stefan Steinerberger

<http://arxiv.org/abs/2305.01774>

Domino tilings of generalized Aztec triangles  
Sylvie Corteel, Frederick Huang, Christian Krattenthaler

<http://arxiv.org/abs/2305.02194>

Generalized hypergeometric coherent states for special functions: mathematical and physical properties  
Isiaka Aremua, Messan Médard Akouetegan, Komi Sodoga, Mahouton Norbert Hounkonnou, Yaogan Mensah

<http://arxiv.org/abs/2305.02928>

Asymptotics of parity biases for partitions into distinct parts via Nahm sums  
Kathrin Bringmann, Siu Hang Man, Larry Rolin, Matthias Storzer

<http://arxiv.org/abs/2305.02989>

Strong  $q$ -analogues for values of the Dirichlet beta function  
Ankush Goswami, Timothy Huber

<http://arxiv.org/abs/2305.03157>

Good Will Hunting's Problem: Counting Homeomorphically Irreducible Trees  
Ira M. Gessel

<http://arxiv.org/abs/2305.03600>

Exact formulas for the fourth and fifth cumulant of the Rosenblatt distribution  
Enno Diekema

<http://arxiv.org/abs/2305.03651>

$(\mathfrak{S}_p \times \mathfrak{S}_q)$ -Invariant Graphical Parking Functions  
Lauren Snider, Catherine Yan

<http://arxiv.org/abs/2305.04302>

Generalized degenerate stirling numbers arising from degenerate boson normal ordering  
Taekyun Kim, Dae San Kim, Hye Kyung Kim

<http://arxiv.org/abs/2305.05476>

Rational extensions of the Dunkl oscillator in the plane and exceptional orthogonal polynomials  
C. Quesne

<http://arxiv.org/abs/2305.05995>

A sufficient condition for  $(\alpha, \beta)$  Somos 4 Hankel determinants  
Ying Wang, Zihao Zhang

<http://arxiv.org/abs/2305.06031>

A facial order for torsion classes  
Eric J. Hanson

<http://arxiv.org/abs/2305.06717>

On a generalization of Jacobi's elegantissima  
Luc Haine

<http://arxiv.org/abs/2305.08472>

Splitting Appell functions in terms of single quotients of theta functions  
Eric T. Mortenson, Dilshod Urazov

<http://arxiv.org/abs/2305.09029>

Log-concavity and log-convexity of series containing multiple Pochhammer symbols  
Dmitrii Karp, Yi Zhang

<http://arxiv.org/abs/2305.09030>

Using Symbolic Computation to Explore Generalized Dyck Paths and Their Areas  
AJ Bu, Doron Zeilberger

<http://arxiv.org/abs/2305.11065>

Uniform approximation of common Gaussian process kernels using equispaced Fourier grids  
Alex Barnett, Philip Greengard, Manas Rachh

<http://arxiv.org/abs/2305.11076>

Blendstrings: an environment for computing with smooth functions  
Robert M. Corless

<http://arxiv.org/abs/2305.13038>

Generalized  $L$ -functions related to the Riemann zeta function  
Kathrin Bringmann, Ben Kane, Srimathi Varadharajan

<http://arxiv.org/abs/2305.13255>

The Geometric Approach to the Classification of Signals via a Maximal Set of Signals  
Leon A. Luxemburg, Steven B. Damelin

<http://arxiv.org/abs/2305.14253>

A heuristic for discrete mean values of the derivative of the Riemann zeta function  
Christopher Hughes, Greg Martin, Andrew Pearce-Crump

<http://arxiv.org/abs/2305.16933>

Representing Piecewise Linear Functions by Functions with Small Arity  
Christoph Koutschan, Bernhard Moser, Anton Ponomarchuk, Josef Schicho

<http://arxiv.org/abs/2305.17278>

One-Parameter Meromorphic Solution of the Degenerate Third Painlevé Equation with Formal Monodromy Parameter  $a = \pm i/2$  Vanishing at the Origin  
A. V. Kitaev, A. Vartanian

<http://arxiv.org/abs/2305.17585>

Curious multisection identities by index factorization  
C. Vignat, M. Milgram

<http://arxiv.org/abs/2305.19025>

Prediction theory in Hilbert Spaces: Operator-valued Szego Theory  
Badr Missaoui, Nicholas H. Bingham

<http://arxiv.org/abs/2305.19128>

Uniform relations between the Gauss-Legendre nodes and weights  
Óscar López Pouso, Javier Segura

<http://arxiv.org/abs/2305.19608>

An inverse spectral problem for non-self-adjoint Jacobi matrices  
Alexander Pushnitski, František Štampach

<http://arxiv.org/abs/2305.19954>

Matrix Orthogonal Polynomials: A Riemann–Hilbert approach  
Amílcar Branquinho, Ana Foulquié–Moreno, Assil Fradi, Manuel Mañas

<http://arxiv.org/abs/2306.01882>

A bivariate  $Q$ -polynomial structure for the non–binary Johnson scheme  
Nicolas Crampé, Luc Vinet, Meri Zaimi, Xiaohong Zhang

<http://arxiv.org/abs/2306.02442>

Elliptic  $A_n$  Selberg integrals  
Seamus P. Albion, Eric M. Rains, S. Ole Warnaar

<http://arxiv.org/abs/2306.02714>

Superspace realizations of the Bannai–Ito algebra  
N. Crampe, H. De Bie, P. Iliev, L. Vinet

<http://arxiv.org/abs/2306.03035>

Double summation addition theorems for Jacobi functions of the first and second kind  
Howard S. Cohl, Roberto S. Costas–Santos, Loyal Durand, Camilo Montoya, Gestur Ólafsson

<http://arxiv.org/abs/2306.03223>

Matrix exceptional Laguerre polynomials  
Erik Koelink, Lucía Morey, Pablo Román

<http://arxiv.org/abs/2306.04638>

Sun’s series via cyclotomic multiple zeta values  
Yajun Zhou

<http://arxiv.org/abs/2306.04921>

A hyperelliptic saga on a generating function of the squares of Legendre polynomials  
Mark van Hoeij, Duco van Straten, Wadim Zudilin

<http://arxiv.org/abs/2306.05158>

Mutually inverse series relating Ferrers and associated Legendre functions and generating functions pertaining to them  
P. Malits

<http://arxiv.org/abs/2306.06681>

New asymptotic representations of the noncentral  $t$ -distribution  
Amparo Gil, Javier Segura, Nico M Temme

<http://arxiv.org/abs/2306.07733>

Shifted Hankel determinants of Catalan numbers and related results II: Backward shifts  
Johann Cigler

<http://arxiv.org/abs/2306.08172>

Sharp Hardy’s Inequalities in Hilbert Spaces  
Dimitar K. Dimitrov, Ivan Gadjev, Mourad E. H. Ismail

<http://arxiv.org/abs/2306.10523>

On Periodic Points in Covering Systems  
Yihan Wang

<http://arxiv.org/abs/2306.10655>

An Infinite Product of the Incomplete Beta Function–type Hypergeometric Function and its Probabilistic Origins

N. S. Witte

<http://arxiv.org/abs/2306.10991>

Modular relations involving generalized digamma functions

Atul Dixit, Sumukha Sathyanarayana, N. Guru Sharan

<http://arxiv.org/abs/2306.11500>

A remark on continued fractions for permutations and D–permutations with a weight  $-1$  per cycle

Bishal Deb, Alan D. Sokal

<http://arxiv.org/abs/2306.11929>

Experimenting with Discrete Dynamical Systems

George Spahn, Doron Zeilberger

<http://arxiv.org/abs/2306.12539>

On the Hill discriminant of Lamé’s differential equation

Hans Volkmer

<http://arxiv.org/abs/2306.12682>

Counting occurrences of patterns in permutations

Andrew R. Conway, Anthony J. Guttmann

<http://arxiv.org/abs/2306.15785>

Two–sided permutation statistics via symmetric functions

Ira M. Gessel, Yan Zhuang

<http://arxiv.org/abs/2306.15847>

Asymptotics and total integrals of the  $P_1^2$  tritronquée solution and its Hamiltonian

Dan Dai, Wen–Gao Long

<http://arxiv.org/abs/2306.16411>

Expansions and characterizations of sieved random walk polynomials

Stefan Kahler

<http://arxiv.org/abs/2306.17085>

Rogers–Ramanujan type identities involving double, triple and quadruple sums

Zhi Li, Liuquan Wang

## Other Relevant OP–SF E–Prints

<http://arxiv.org/abs/2305.00198>

Infinitesimal generators for a family of polynomial processes – an algebraic approach

Jacek Wesołowski, Agnieszka Zięba

<http://arxiv.org/abs/2305.00202>

The resolvent kernel on the discrete circle and twisted cosecant sums

Jay Jorgenson, Anders Karlsson, Lejla Smajlović

<http://arxiv.org/abs/2305.00364>

$\varphi$ - $(k, n)$ -absorbing and  $\varphi$ - $(k, n)$ -absorbing primary hyperideals in a krasner  $(m, n)$ -hyperring  
Mahdi Anbarloei

<http://arxiv.org/abs/2305.00498>

Some series involving harmonic numbers  
Xiaoxia Wang, Haihong He

<http://arxiv.org/abs/2305.00563>

Dickman multiple polylogarithms and the Lindemann–Furry letters  
David Broadhurst, Stephan Ohlmeyer

<http://arxiv.org/abs/2305.00626>

On two-term hypergeometric recursions with free lower parameters  
John M. Campbell, Paul Levrie

<http://arxiv.org/abs/2305.00701>

First integrals of nonlinear differential equations from nonlocal constants  
Mattia Scomparin

<http://arxiv.org/abs/2305.00789>

A construction of the polylogarithm motive  
Clément Dupont, Javier Fresán

<http://arxiv.org/abs/2305.00846>

On ordered beta distribution and the generalized incomplete beta function  
Mayad Al-Saidi, Alexey Kuznetsov, Mikhail Nediak

<http://arxiv.org/abs/2305.01262>

New developments toward the Gonek Conjecture on the Hurwitz zeta-function  
Masahiro Mine

<http://arxiv.org/abs/2305.01369>

The spectrum of the Poincaré operator in an ellipsoid  
Yves Colin de Verdière, Jérémie Vidal

<http://arxiv.org/abs/2305.01460>

$p$ -adic generalizations of hyper-elliptic functions  
Yaacov Kopeliovich

<http://arxiv.org/abs/2305.01829>

The merging operation and  $(d - i)$ -simplicial  $i$ -simple  $d$ -polytopes  
Isabella Novik, Hailun Zheng

<http://arxiv.org/abs/2305.01950>

The Chow–Kontsevich dilogarithm  
Sinan Ünver

<http://arxiv.org/abs/2305.02754>

A lower bound for the beta function  
Tiehong Zhao, Miaokun Wang



<http://arxiv.org/abs/2305.03367>

Orthogonal Intertwiners for Infinite Particle Systems In The Continuum  
Stefan Wagner

<http://arxiv.org/abs/2305.03370>

More properties of  $(\beta, \gamma)$ -Chebyshev functions and points  
Stefano De Marchi, Giacomo Elefante, Francesco Marchetti, Jean-Zacharie Mariethoz

<http://arxiv.org/abs/2305.03951>

The Riemann Hypothesis for period polynomials of cusp forms  
William Craig, Wissam Raji

<http://arxiv.org/abs/2305.03978>

40 Bilinear Relations of  $q$ -Painlevé VI from  $N = 4$  Super Chern-Simons Theory  
Sanefumi Moriyama, Tomoki Nosaka

<http://arxiv.org/abs/2305.03986>

First Derivative of Automorphic Function of Triangle Groups  
Md. Shafiul Alam

<http://arxiv.org/abs/2305.04071>

The reflection coefficient of a fractional reflector  
Laurent Demanet, Olivier Lafitte

<http://arxiv.org/abs/2305.04131>

Asymptotics of Generalized Bessel Functions and Weight Multiplicities via Large Deviations of Radial Dunkl Processes  
Jiaoyang Huang, Colin McSwiggen

<http://arxiv.org/abs/2305.04240>

Painlevé/CFT correspondence on a torus  
Harini Desiraju

<http://arxiv.org/abs/2305.04251>

Mellin definition of the fractional Laplacian  
Gianni Pagnini, Claudio Runfola

<http://arxiv.org/abs/2305.04404>

On a class of elliptic orthogonal polynomials and their integrability  
Harini Desiraju, Tomas Lasic Latimer, Pieter Roffelsen

<http://arxiv.org/abs/2305.04472>

KP hierarchy, affine Yangian and  $W_{1+\infty}$  algebra  
Na Wang

<http://arxiv.org/abs/2305.04488>

Zak transform associated with the Weyl transform and the system of twisted translates on  $\mathbb{R}^{2n}$   
Radha Ramakrishnan, Rabeetha Velsamy

<http://arxiv.org/abs/2305.04633>

Fractal derivatives, fractional derivatives and  $q$ -deformed calculus  
Airtton Deppman, Eugenio Megias, Roman Pasechnik

<http://arxiv.org/abs/2305.04781>

An extension of Schur's irreducibility result  
Ankita Jindal, Sudesh Kaur Khanduja

<http://arxiv.org/abs/2305.04786>

On the period of Pell–Narayana sequence in some groups  
Bahar Kulođlu, Engin Özkan, Marin Marin

<http://arxiv.org/abs/2305.04903>

Newton–Okounkov bodies and minimal models for cluster varieties  
Lara Bossinger, Man–Wai Cheung, Timothy Magee, Alfredo Nájera Chávez

<http://arxiv.org/abs/2305.04906>

Quantum Lefschetz theorem revisited  
Jun Wang

<http://arxiv.org/abs/2305.04999>

Enhanced computation of the proximity operator for perspective functions  
Luis M. Briceño–Arias, Cristóbal Vivar–Vargas

<http://arxiv.org/abs/2305.06069>

The Wigner–Vlasov formalism for time–dependent quantum oscillator  
E.E. Perepelkin, B.I. Sadovnikov, N.G. Inozemtseva, A.A. Korepanova

<http://arxiv.org/abs/2305.06107>

On real zeros of the Hurwitz zeta function  
Karin Ikeda

<http://arxiv.org/abs/2305.06197>

Parametric Dynamic Mode Decomposition for nonlinear parametric dynamical systems  
Shuwen Sun, Lihong Feng, Hoon Seng Chan, Tamara Miličić, Tanja Vidaković–Koch, Peter Benner

<http://arxiv.org/abs/2305.06623>

Hankel determinants and Jacobi continued fractions for  $q$ –Euler numbers  
Shane Chern, Lin Jiu

<http://arxiv.org/abs/2305.06761>

Isoperiodic foliation of the stratum  $\mathcal{H}(1, 1, -2)$   
Gianluca Faraco, Guillaume Tahar, Yongquan Zhang

<http://arxiv.org/abs/2305.06766>

On the Convergence of Random Fourier–Jacobi Series in  $L^p(d\mu_{\zeta, \eta})$  Space  
Partiswari Maharana Sabita Sahoo

<http://arxiv.org/abs/2305.06998>

The Fueter–Sce mapping and the Clifford–Appell polynomials  
Antonino De Martino, Kamal Diki, Ali Guzmán Adán

<http://arxiv.org/abs/2305.07412>

An asymptotic expansion for a Lambert series associated to Siegel cusp forms  
Babita, Abhash Kumar Jha, Abhishek Juyal, Bibekananda Maji

<http://arxiv.org/abs/2305.07860>

Szegő-type theorems on compact Abelian groups and spectral approximations for multiplicative Toeplitz matrices

Kunyu Guo, Dilong Li, Qi Zhou

<http://arxiv.org/abs/2305.07869>

Some new curious congruences involving multiple harmonic sums

Rong Ma, Ni Li

<http://arxiv.org/abs/2305.07966>

Positive formula for Jack polynomials, Jack characters and proof of Lassalle's conjecture

Houcine Ben Dali, Maciej Dołęga

<http://arxiv.org/abs/2305.08074>

Orthogonal polynomial approximation and Extended Dynamic Mode Decomposition in chaos

Caroline L. Wormell

<http://arxiv.org/abs/2305.08101>

The generalized Zwegers'  $\mu$ -function and transformation formulas for the bilateral basic hypergeometric series

Genki Shibukawa, Satoshi Tsuchimi

<http://arxiv.org/abs/2305.08364>

Emergence of the Gambier equation in cosmology

D. Batic, P. Guha, A. Ghose Choudhury

<http://arxiv.org/abs/2305.08554>

Universality in Binary Black Hole Dynamics: An Integrability Conjecture

José Luis Jaramillo, Badri Krishnan, Carlos F. Sopuerta

<http://arxiv.org/abs/2305.08581>

Multivariate Krawtchouk polynomials as Birth and Death polynomials

Ryu Sasaki

<http://arxiv.org/abs/2305.08618>

A note on Appell's functions related to the denominators of affine Lie superalgebras  $\widehat{sl}(2|1)$  and  $\widehat{osp}(3|2)$

Minoru Wakimoto

<http://arxiv.org/abs/2305.08751>

Deviation of the rank and crank modulo 11

Nikolay Borozenets

<http://arxiv.org/abs/2305.08862>

Transition Probabilities and Almost Periodic Functions

S. O. Juriaans, P. C. Queiroz

<http://arxiv.org/abs/2305.08976>

Eigenvalues of truncated unitary matrices: disk counting statistics

Yacin Ameur, Christophe Charlier, Philippe Moreillon

<http://arxiv.org/abs/2305.09170>

Multivariate Hahn polynomials, a Birth and Death approach

Ryu Sasaki

<http://arxiv.org/abs/2305.09217>

Wall-crossing formula for framed quiver moduli  
Ryo Ohkawa

<http://arxiv.org/abs/2305.09227>

On  $n^{\text{th}}$  order Euler polynomials of degree  $n$  that are Eisenstein  
Michael Filaseta, Thomas Luckner

<http://arxiv.org/abs/2305.09340>

Bézout identities and control of the heat equation  
François Ollivier

<http://arxiv.org/abs/2305.09670>

On the zeros of Riemann's Xi Function  
Akhila Raman

<http://arxiv.org/abs/2305.10858>

$H^p$  theory of separately  $(\alpha, \beta)$ -harmonic functions in the unit polydisc  
Jelena Gajic, Milos Arsenovic, Miodrag Mateljevic

<http://arxiv.org/abs/2305.11492>

Results on the Non-Vanishing of Derivatives of L-Functions of Vector-Valued Modular Forms  
Subong Lim, Wissam Raji

<http://arxiv.org/abs/2305.11836>

Fundamental solutions and critical Lane-Emden exponents for nonlinear integral operators in cones  
Gabrielle Nornberg, Disson dos Prazeres, Alexander Quaas

<http://arxiv.org/abs/2305.12007>

Ramanujan sums and rectangular power sums  
John Shareshian, Sheila Sundaram

<http://arxiv.org/abs/2305.12051>

Regulator of the Hesse cubic curves and hypergeometric functions  
Yusuke Nemoto

<http://arxiv.org/abs/2305.12210>

The dual reciprocity boundary elements method for one-dimensional nonlinear parabolic partial differential equations  
Peyman Alipour

<http://arxiv.org/abs/2305.12241>

Analytic continuation of better-behaved GKZ systems and Fourier-Mukai transforms  
Zengrui Han

<http://arxiv.org/abs/2305.12754>

$q$ -difference equation satisfied by the universal mock theta functions  
Satoshi Tsuchimi

<http://arxiv.org/abs/2305.13007>

On the number of roots of Sturm-Liouville random sums  
Federico Dalmao, José R. León

<http://arxiv.org/abs/2305.13039>

On the Study of the Klein–Gordon Equation in the Dunkl Setting  
Mohamed Gaidi, Mounir Bedhiafi

<http://arxiv.org/abs/2305.14015>

The Fan–Taussky–Todd inequalities and the Lumer–Phillips theorem  
Benedict Bauer, Stefan Gerhold

<http://arxiv.org/abs/2305.14367>

A series of Ramanujan, two–term dilogarithm identities and some Lucas series  
Kunle Adegoke, Robert Frontczak

<http://arxiv.org/abs/2305.14393>

Finite Sums and Products involving Special Functions  
Robert Reynolds

<http://arxiv.org/abs/2305.14664>

Two Matrix Model, the Riemann Hypothesis and Master Matrix Obstruction  
Michael McGuigan

<http://arxiv.org/abs/2305.14988>

Some Identities of Ramanujan’s  $q$ –Continued Fractions of Order Fourteen and Twenty–Eight, and Vanishing Coefficients  
Shraddha Rajkhowa, Nipen Saikia

<http://arxiv.org/abs/2305.15514>

Rotational cmc surfaces in terms of Jacobi elliptic functions  
Denis Polly

<http://arxiv.org/abs/2305.15806>

Expansion of generalized Stieltjes constants in terms of derivatives of Hurwitz zeta–functions  
M. Prévost

<http://arxiv.org/abs/2305.15882>

A filtered Chebyshev spectral method for conservation laws on network  
Sabrina Francesca Pellegrino

<http://arxiv.org/abs/2305.15970>

Boundedness of zeros of Sobolev orthogonal polynomials via generalized eigenvalues  
C. Escribano, R. Gonzalo

<http://arxiv.org/abs/2305.16184>

Analytic continuation of  $\ell$ –generalized Fibonacci zeta function  
Dilip Kumar Sahoo, Nabin Kumar Meher

<http://arxiv.org/abs/2305.16218>

Non–vanishing of multiple zeta values for higher genus curves over finite fields  
Daichi Matsuzuki

<http://arxiv.org/abs/2305.16537>

Functional equations and gamma factors of local zeta functions for the metaplectic cover of  $SL_2$   
Kazuki Oshita, Masao Tsuzuki

<http://arxiv.org/abs/2305.16654>

Oscillating asymptotics for a Nahm–type sum and conjectures of Andrews  
Amanda Folsom, Joshua Males, Larry Rolen, Matthias Storzer

<http://arxiv.org/abs/2305.16769>

ASEP proofs of some partition identities and the blocking stationary behaviour of second class particles  
Daniel Adams, Márton Balázs, Jessica Jay

<http://arxiv.org/abs/2305.17107>

Determination of the symmetry group for some QRT roots  
Giorgio Gubbiotti, Yang Shi

<http://arxiv.org/abs/2305.17123>

An Analysis of the Johnson–Lindenstrauss Lemma with the Bivariate Gamma Distribution  
Jason Bernstein, Alec M. Dunton, Benjamin W. Priest

<http://arxiv.org/abs/2305.17646>

Direct Integral Pseudospectral and Integral Spectral Methods for Solving a Class of Infinite Horizon Optimal Output Feedback Control Problems Using Rational and Exponential Gegenbauer Polynomials  
Kareem T. Elgindy, Hareth M. Refat

<http://arxiv.org/abs/2305.17747>

Tilted biorthogonal ensembles, Grothendieck random partitions, and determinantal tests  
Svetlana Gavrilova, Leonid Petrov

<http://arxiv.org/abs/2305.17912>

On  $q$ –Painlevé VI and the geometry of Segre surfaces  
Pieter Roffelsen

<http://arxiv.org/abs/2305.17962>

Matrix–valued  $\theta$ –deformed bi–orthogonal polynomials, Non–commutative Toda theory and Bäcklund transformation  
Claire Gilson, Shi–Hao Li, Ying Shi

<http://arxiv.org/abs/2305.18252>

On MaxCut and the Lovász theta function  
Igor Balla, Oliver Janzer, Benny Sudakov

<http://arxiv.org/abs/2305.18546>

Sharp Gaussian decay for the one–dimensional harmonic oscillator  
Danylo Radchenko, João P. G. Ramos

<http://arxiv.org/abs/2305.18669>

Determination of normalized extremal quasimodular forms of depth 1 with integral Fourier coefficients  
Tomoaki Nakaya

<http://arxiv.org/abs/2305.18672>

Universality theorems of the Selberg zeta functions for arithmetic groups  
Yasufumi Hashimoto

<http://arxiv.org/abs/2305.18833>

Gaussian Unitary Ensembles with Fisher–Hartwig Singularities and Generalized Painlevé IV Equation  
Xinyu Mu, Shulin Lyu

<http://arxiv.org/abs/2305.19368>

Hypergeometric Sheaves and General Linear Groups  
Lee Tae Young

<http://arxiv.org/abs/2305.19616>

Rodrigues formula and linear independence for values of hypergeometric functions with parameters vary  
Makoto Kawashima

<http://arxiv.org/abs/2305.19680>

Spectral theory of Jacobi operators with increasing coefficients. The critical case  
D. R. Yafaev

<http://arxiv.org/abs/2305.19852>

Generalised unitary group integrals of Ingham–Siegel and Fisher–Hartwig type  
Gernot Akemann, Noah Aygün, Tim R. Würfel

<http://arxiv.org/abs/2305.19975>

The Pieri formulas and the Littlewood–Richardson rule for Schur multiple zeta functions  
Shutaro Nakaoka

<http://arxiv.org/abs/2306.00161>

On the equidistribution properties of patterns in prime numbers Jumping Champions, metaanalysis of properties as Low–Discrepancy Sequences, and some conjectures based on Ramanujan’s master theorem and the zeros of Riemann’s zeta function  
Arturo Ortiz–Tapia

<http://arxiv.org/abs/2306.00215>

An Elliptic Generalization of  $A_1$  Spherical DAHA at  $K = 2$   
S. Arthamonov, Sh. Shakirov

<http://arxiv.org/abs/2306.00460>

Spirals of Riemann’s Zeta–Function – Curvature, Denseness, and Universality –  
Athanasios Sourmelidis, Jörn Steuding

<http://arxiv.org/abs/2306.01331>

Quantum dilogarithms over local fields and invariants of 3–manifolds  
Stavros Garoufalidis, Rinat Kashaev

<http://arxiv.org/abs/2306.01767>

On Schur’s irreducibility results and generalised  $\varphi$ –Hermite polynomials  
Anuj Jakhar

<http://arxiv.org/abs/2306.02241>

Visible Point Partition Identities for Polylogarithms, and Parametric Euler Sums  
Geoffrey B. Campbell

<http://arxiv.org/abs/2306.02554>

The Voronoi Summation Formula for  $GL_n$  via the Godement–Jacquet Zeta Integrals  
Dihua Jiang, Zhaolin Li

<http://arxiv.org/abs/2306.02635>

Supercongruences arising from a  ${}_7F_6$  hypergeometric transformation formula  
Chen Wang

<http://arxiv.org/abs/2306.02641>

On some conjectural series containing binomial coefficients and harmonic numbers  
Chuanan Wei

<http://arxiv.org/abs/2306.04659>

Monotonicity rules for the ratio of two function series and two integral transforms  
Zhong-Xuan Mao, Jing-Feng Tian

<http://arxiv.org/abs/2306.04799>

An unconditional Montgomery Theorem for Pair Correlation of Zeros of the Riemann Zeta Function  
Siegfred Alan C. Baluyot, Daniel Alan Goldston, Ade Irma Suriajaya, Caroline L. Turnage-Butterbaugh

<http://arxiv.org/abs/2306.04807>

On a smoothed average of the number of Goldbach representations  
Daniel A. Goldston, Ade Irma Suriajaya

<http://arxiv.org/abs/2306.05371>

New results on the associated Meixner, Charlier, Laguerre, and Krawtchouk polynomials  
Khalid Ahbli

<http://arxiv.org/abs/2306.06214>

The Bicomplex-Real Calculus and Applications to Bicomplex Hermite-Itô Polynomials  
Daniel Alpay, Kamal Diki, Mihaela Vajiac

<http://arxiv.org/abs/2306.06444>

On the  $D_\omega$ -classical orthogonal polynomials  
Khalifa Douak

<http://arxiv.org/abs/2306.06623>

Commutative families in  $W_\infty$ , integrable many-body systems and hypergeometric  $\tau$ -functions  
A. Mironov, V. Mishnyakov, A. Morozov, A. Popolitov

<http://arxiv.org/abs/2306.06890>

On the irreducibility of extended Laguerre Polynomials  
Anuj Jakhar, Srinivas Kotyada, Arunabha Mukhopadhyay

<http://arxiv.org/abs/2306.07062>

Non-integrability of a four-dimensional Painlevé system of type  $D_5^{(1)}$   
Tsvetana Stoyanova

<http://arxiv.org/abs/2306.07063>

Rational Hermite-Padé Approximants vs Padé Approximants. I. Numerical Results  
Nikolay R. Ikononov, Leonid A. Knizhnerman, Sergey P. Suetin

<http://arxiv.org/abs/2306.07073>

Painlevé type asymptotics of defocusing mKdV equation with a nonzero background  
Zhaoyu Wang, Taiyang Xu, Engui Fan



<http://arxiv.org/abs/2306.07431>

Deformed  $(s, t)$ -Binomial Formula applied to the  $(s, t)$ -analogues of Elementary functions, Gamma Function and Binomial Series

Ronald Orozco López

<http://arxiv.org/abs/2306.07648>

Jacob's ladders, almost linear increments of the Hardy-Littlewood integral (1918) and their relations to the Selberg's formula (1946) and the Fermat-Wiles theorem

Jan Moser

<http://arxiv.org/abs/2306.07777>

Simultaneous extreme values of zeta and  $L$ -functions

Winston Heap, Junxian Li

<http://arxiv.org/abs/2306.08022>

On an Alternating Double Sum of a Triple Product of Aerated Binomial Coefficients

Richard J. Mathar

<http://arxiv.org/abs/2306.08389>

On Derkachov-Manashov  $R$ -matrices for the principal series of unitary representations

Yury A. Neretin

<http://arxiv.org/abs/2306.08411>

The MacWilliams Identity for the Hermitian Rank Metric

Izzy Friedlander

<http://arxiv.org/abs/2306.08493>

A Note on Twisted Moments of Dirichlet  $L$ -functions

J. C. Andrade, J. MacMillan

<http://arxiv.org/abs/2306.08831>

Integrality of the higher Rademacher symbols

Cormac O'Sullivan

<http://arxiv.org/abs/2306.09102>

The Average Number of Goldbach Representations and Zero-Free Regions of the Riemann Zeta-Function

Keith Billington, Maddie Cheng, Jordan Schettler, Ade Irma Suriajaya

<http://arxiv.org/abs/2306.10393>

Many  $p$ -adic odd zeta values are irrational

Li Lai, Johannes Sprang

<http://arxiv.org/abs/2306.10446>

Hurwitz spaces, Nichols algebras, and Igusa zeta functions

Kevin Chang

<http://arxiv.org/abs/2306.10653>

Weierstrass elliptic functions for the pendulum

Oliver Knill

<http://arxiv.org/abs/2306.10680>

Explicit bounds for the Riemann zeta function and a new zero-free region

Chiara Bellotti

<http://arxiv.org/abs/2306.11381>

Computation of the Wright function from its integral representation  
Dimitar Prodanov

<http://arxiv.org/abs/2306.11718>

MultiHypExp: A Mathematica Package For Expanding Multivariate Hypergeometric Functions In Terms Of Multiple Polylogarithms  
Souvik Bera

<http://arxiv.org/abs/2306.11875>

Quartic Gauss sums over primes and metaplectic theta functions  
Chantal David, Alexander Dunn, Alia Hamieh, Hua Lin

<http://arxiv.org/abs/2306.12263>

Local Statistics in Normal Matrix Models with Merging Singularity  
Torben Krüger, Seung-Yeop Lee, Meng Yang

<http://arxiv.org/abs/2306.12265>

Spectral quantization of discrete random walks on half-line, and orthogonal polynomials on the unit circle  
Adam Doliwa, Artur Siemaszko

<http://arxiv.org/abs/2306.12399>

Character analogues of Cohen type identities and related Voronoi summation formulas  
Debika Banerjee, Khyati Khurana

<http://arxiv.org/abs/2306.12877>

Trigonometric analogue of the identities associated with twisted sums of divisor functions  
Debika Banerjee, Khyati Khurana

<http://arxiv.org/abs/2306.13289>

Explicit bounds for the Riemann zeta-function on the 1-line  
Ghaith A. Hiary, Nicol Leong, Andrew Yang

<http://arxiv.org/abs/2306.13309>

Partitions with parts separated by parity: conjugation, congruences and the mock theta functions  
Shishuo Fu, Dazhao Tang

<http://arxiv.org/abs/2306.13619>

Sampling in the shift-invariant space generated by the bivariate Gaussian function  
José Luis Romero, Alexander Ulanovskii, Ilya Zlotnikov

<http://arxiv.org/abs/2306.13635>

Factoring determinants and applications to number theory  
Estelle Basor, Brian Conrey

<http://arxiv.org/abs/2306.14107>

A Riemann-Hilbert approach to skew-orthogonal polynomials of symplectic type  
Alex Little

<http://arxiv.org/abs/2306.14166>

Random normal matrices: eigenvalue correlations near a hard wall

Yacin Ameur, Christophe Charlier, Joakim Cronvall

<http://arxiv.org/abs/2306.14371>

Shuffle formula in science fiction for Macdonald polynomials

Donghyun Kim, Seung Jin Lee, Jaeseong Oh

<http://arxiv.org/abs/2306.14625>

On the relation between quantum walks and absolute zeta functions

Norio Konno

<http://arxiv.org/abs/2306.14656>

Discrete Bessel functions and discrete wave equation

Amar Bašić, Lejla Smajlović, Zenan Šabanac

<http://arxiv.org/abs/2306.14835>

Asymptotics of the deformed higher order Airy-kernel determinants and applications

Jun Xia, Yi-Fan Hao, Shuai-Xia Xu, Lun Zhang, Yu-Qiu Zhao

<http://arxiv.org/abs/2306.15936>

Finite field analogues of integral representations of Appell-Lauricella functions using confluent hypergeometric functions

Akio Nakagawa

<http://arxiv.org/abs/2306.15972>

On  $q$ -Gevrey asymptotics for logarithmic type solutions in singularly perturbed  $q$ -difference-differential equations

Alberto Lastra, Stéphane Malek

<http://arxiv.org/abs/2306.16679>

A short note on strong convergence of  $q$ -Gaussians

Akihiro Miyagawa

<http://arxiv.org/abs/2306.16720>

Asymptotic analysis of the characteristic polynomial for the Elliptic Ginibre Ensemble

Quentin François, David García-Zelada

<http://arxiv.org/abs/2306.17677>

Dunkl symplectic algebra in generalized Calogero models

Tigran Hakobyan

Topic #8 ——— OP – SF Net 30.4 ——— July 15, 2023

From: OP-SF Net Editors

Subject: Submitting contributions to OP-SF NET and SIAM-OPSF (OP-SF Talk)

To contribute a news item to OP-SF NET, send e-mail to one of the OP-SF Editors

[howard.cohl@nist.gov](mailto:howard.cohl@nist.gov), or [spost@hawaii.edu](mailto:spost@hawaii.edu).

Contributions to OP-SF NET 30.5 should be sent by September 1, 2023.

OP-SF NET is the electronic newsletter of the SIAM Activity Group on Special Functions and Orthogonal Polynomials (SIAG/OPSF). We disseminate your contributions on anything of interest to the special

functions and orthogonal polynomials community. This includes announcements of conferences, forthcoming books, new software, electronic archives, research questions, and job openings as well as news about new appointments, promotions, research visitors, awards and prizes. OP-SF Net is transmitted periodically through a post to OP-SF Talk which is currently managed and moderated by Howard Cohl ([howard.cohl@nist.gov](mailto:howard.cohl@nist.gov)). Anyone wishing to be included in the mailing list (SIAG/OPSF members and non-members alike) should send an email expressing interest to him. Bonita Saunders also posts the Newsletter through SIAM Engage (SIAG/OPSF) which is received by all SIAG/OPSF members.

OP-SF Talk is a listserv associated with SIAG/OPSF which facilitates communication among members, non-members and friends of the Activity Group. To post an item to the listserv, send e-mail to [howard.cohl@nist.gov](mailto:howard.cohl@nist.gov).

WWW home page of this Activity Group:

<http://math.nist.gov/opsf>

Information on joining SIAM and this activity group: [service@siam.org](mailto:service@siam.org)

The elected Officers of the Activity Group (2020–2022\*) are:

Peter Alan Clarkson, Chair

Luc Vinet, Vice Chair

Andrei Martínez-Finkelshtein, Program Director

Teresa E. Pérez, Secretary and SIAM Engage (SIAG/OPSF) moderator

The appointed officers are:

Howard Cohl, OP-SF NET co-editor

Sarah Post, OP-SF NET co-editor

Bonita Saunders, Webmaster and SIAM Engage (SIAG/OPSF) moderator

\*As of the date of the publication of OP-SF NET 30.4, the SIAG/OPSF elections have not occurred.

## Topic #9 ——— OP – SF Net 30.4 ——— July 15, 2023

From: OP-SF Net Editors

Subject: Thought of the Month by **Tom H. Koornwinder**

“The addition formula for ultraspherical (or Gegenbauer) polynomials is usually ascribed to Gegenbauer in (1874)<sup>1</sup>. However, it is already stated and proved by Allé in 1865<sup>2</sup>. The subsequent proofs by Gegenbauer in 1874 and 1893<sup>3</sup>, and by Heine [10, p. 455] in (1878)<sup>4</sup> do not mention Allé’s result.”

**Tom H. Koornwinder**, *Dual Addition Formulas Associated with Dual Product Formulas*, Chapter 19, pp. 373–392, *Frontiers in Orthogonal Polynomials and  $q$ -Series*, Ed. M. Zuhair Nashed & Xin Li, *Contemporary Mathematics and Its Applications*, Vol. 1, 2018, [arXiv:1607.06053v5](https://arxiv.org/abs/1607.06053v5).

Comment by **Claude Brezinski** and **Michela Redivo-Zaglia** on July 4, 2023: I found that Gegenbauer polynomials were also given by **Robert Most**, Ueber die Differentialgleichungen der Kugelfunctionen, *J. Reine Angew. Math.*, 70 (1869) 163–168.

---

<sup>1</sup>L. Gegenbauer. Über einige bestimmte Integrale. *Sitzungsberichte der Kaiserlichen Akademie der Wissenschaften. Mathematische-Naturwissenschaftliche Classe.*, 70:433–443, 1874.

<sup>2</sup>M. Allé. Über die Eigenschaften derjenigen Gattung von Functionen, welche in der Entwicklung von  $(1 - 2qx + q^2)^{-\frac{m}{2}}$  nach aufsteigenden Potenzen von  $q$  auftreten, und über die Entwicklung des Ausdrucks  $\{1 - 2q[\cos \theta \cos \theta' + \sin \theta \sin \theta' \cos(\psi - \psi')] + q^2\}^{-\frac{m}{2}}$ . *Sitzungsberichte der mathematisch-naturwissenschaftlichen Classe der kaiserlichen Akademie der Wissenschaften Wien*, 51:429–458, 1865.

<sup>3</sup>L. Gegenbauer. Das Additionstheorem der Functionen  $C_n^\nu(x)$ . *Sitzungsberichte der Kaiserlichen Akademie der Wissenschaften. Mathematische-Naturwissenschaftliche Classe.*, 102:942–950, 1893.

<sup>4</sup>E. Heine. *Handbuch der Kugelfunctionen, Theorie und Anwendungen* (volume 1). Druck und Verlag von G. Reimer, Berlin, 1878.